

Dynamic Ecosystem-FINance-Economy (DEFINE) model, technical description and data, version 1.0

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Contents

1. Introduction	2
2. Structure of the model.....	3
2.1 Ecosystem.....	6
2.1.1 Matter, recycling and waste.....	8
2.1.2 Energy.....	10
2.1.3 Emissions and climate change	10
2.1.4 Ecological efficiency and technology	12
2.2 Macroeconomy and financial system.....	13
2.2.1 Output determination and damages.....	15
2.2.2 Firms	19
2.2.3 Households	25
2.2.4 Commercial banks.....	28
2.2.5 Government sector.....	29
2.2.6 Central banks	30
3. Baseline scenario.....	32
4. Symbols and values	34
References.....	40

1. Introduction

This document presents the technical details of the DEFINE (Dynamic Ecosystem-FINance-Economy) model (version 1.0). DEFINE is a global stock-flow-fund ecological macroeconomic model that analyses the interactions between the ecosystem, the financial system and the macroeconomy. It incorporates explicitly the laws of thermodynamics, the carbon cycle, the climate change damages, the waste generation process, the endogeneity of money and the impact of finance on economic activity. DEFINE produces various scenarios for the future of the ecosystem and the global economy. It is also used to evaluate the long-run effects of various types of environmental policies and strategies, paying particular attention to the role of finance.

DEFINE combines the post-Keynesian stock-flow consistent (SFC) approach developed by Godley and Lavoie (2007) with the flow-fund model of Georgescu-Roegen (1971, ch. 9; 1979; 1984). The key innovation of the post-Keynesian SFC approach is the integration of accounting into dynamic macro modelling. This integration permits the detailed exploration of the links between the real and the financial spheres of the macroeconomy. The flow-fund model of Georgescu-Roegen encapsulates the fundamental propositions of ecological economics. The model relies on a multi-process matrix that depicts the physical inflows and outflows that take place during the various economic processes, drawing explicitly on the First and the Second Law of Thermodynamics.

The combination of the SFC approach with the flow-fund model of Georgescu-Roegen provides an integrated approach to the combined analysis of physical and monetary stocks and flows. In DEFINE this analysis relies on four matrices: 1) the physical flow matrix; 2) the physical stock-flow matrix; 3) the transactions flow matrix; 4) the balance sheet matrix. The first matrix is a simplified version of the matrix that Georgescu-Roegen's used in his flow-fund model. The second matrix captures the dynamic interaction between physical stocks and flows and is a natural extension of the physical flow matrix. The third matrix and the fourth matrix describe the changes in the stocks and flows of the macroeconomic and the financial system, following the traditional formulations in the SFC literature.

In line with the post-Keynesian tradition, output in the model is determined by aggregate demand. However, supply-side constraints might arise primarily due to environmental

problems. This is formalised by using a Leontief-type production function that specifies the supply-determined output drawing on Georgescu-Roegen's distinction between stock-flow and fund-service resources.¹ It is assumed that environmental problems affect in a different way each type of resources. Depletion problems affect the stock-flow resources (i.e. non-renewable energy and material resources can be exhausted) while degradation problems, related to climate change and the accumulation of hazardous waste, damage the fund-service resources (by destroying them directly or by reducing their productivity). Climate change and its damages are modelled using standard specifications from the integrated assessment modelling literature (see Nordhaus and Sztorc, 2013). However, a key departure from this literature is that global warming damages do not affect an output determined via a neoclassical production function. Instead, they influence the fund-service resources of our Leontief-type production function and the components of aggregate demand.

Section 2 describes the matrices and the equations of the model. *Section 3* presents the key features of the baseline scenario used in this version. *Section 4* reports all the symbols of the model, the data sources and the values used for parameters and variables.

2. Structure of the model

DEFINE consists of two big blocks. The first block is the ecosystem block which includes equations about (i) matter, recycling and waste, (ii) energy, (iii) emissions and climate change and (iv) ecological efficiency and technology. The second block is the macroeconomy and financial system block which includes equations about (i) output determination, (ii) firms, (iii) households, (iii) banks, (iv) the government sector and (v) the central banks.

It is assumed that there is one type of material good that can be used for durable consumption and (conventional and green) investment purposes. Four matter/energy transformation processes are necessary for the production of this good and all of them require capital and labour. First, matter (non-metallic minerals and metal ores) has to be extracted from the ground and has to be transformed into a form that can be used as an input in the production.

¹ The stock-flow resources (non-renewable energy and material resources) are transformed into what they produce (including by-products), can theoretically be used at any rate desired and can be stockpiled for future use. The fund-service resources (labour, capital and Ricardian land) are not embodied in the output produced, can be used only at specific rates and cannot be stockpiled for future use. Crucially, these types of resources are not substitutable: they are both necessary for the production process.

Second, useful energy has to be generated based on non-renewable sources (e.g. oil, gas and coal) or renewable sources (e.g. sun, wind).² Third, recycling has to take place. Every year a part of the capital stock and the durable consumption goods that have been accumulated in the socio-economic system are demolished/discarded; the material content of these accumulated capital goods and durable consumption goods is called socio-economic stock.³ A proportion of this demolished/discarded socio-economic stock is recycled and is used as an inflow in the production of the final good. This means that not all of the matter that is necessary for the production of the good has to be extracted from the ground. Fourth, the final good needs to be produced using material and energy inflows from the other processes.

Crucially, all these four processes, in combination with the functioning of the whole socio-economic system, generate by-products. In particular, industrial CO₂ emissions are produced as a result of the combustion of fossil fuels. Energy is dissipated in all transformation processes; this energy cannot be used again. In addition, the demolished/discarded socio-economic stock that is not recycled becomes waste. Part of this waste is hazardous and can have adverse effects on the health of the population.

Since the model focuses on the aggregate effects of production, all the above-mentioned processes have been consolidated and are presented as part of the total production process. An unconsolidated formulation of the production process would make the model and its calibration much more complicated without changing the substance of the analysis that we pursue here. However, such an unconsolidated version would be useful for the analysis of intra-firm dynamics and could be the subject of future extensions of the model.

Although capital, labour, energy and matter are all necessary in the transformation processes, these resources do not directly determine the level of production as long as they are not scarce: in the absence of scarcity, the level of production is demand-determined, in line with the post-Keynesian tradition. However, if any of these resources is not sufficient to satisfy the demand, production is directly affected by resource scarcity. In particular, we assume that,

² For brevity, the energy produced from (non-)renewable sources is henceforth referred to as (non-)renewable energy. For simplicity, the model does not incorporate energy and matter from biomass. However, the figure used for the share of renewable energy in our calibrations includes bioenergy to facilitate comparison with other studies.

³ This is a term used in material flow analysis (see e.g. Krausmann et al., 2015). In general, socio-economic stock also includes animal livestock and humans. However, these stocks (whose mass remains relatively stable over time) are not included in our analysis. As will be explained below, socio-economic stock is measured in Gigatonnes.

under supply-side constraints, consumption and investment demand might decline. Moreover, although all these resources are necessary for the production of goods based on our Leontief-type production function (i.e. there is imperfect substitutability), their relative use changes because of technological progress.

A crucial distinction is made between green capital and conventional capital. Compared to conventional capital, green capital is characterised by lower energy intensity, lower material intensity and higher recycling rate. Moreover, green capital produces energy using renewable sources, while conventional capital produces energy using the non-renewable sources. Hence, the use of green capital is conducive to a low-carbon economy.⁴ As the proportion of green capital to conventional capital increases, the goods consumed by households are produced in a more environmentally friendly way. However, we do not make a distinction between conventional and green consumption goods. This means that households' environmental preferences do not have a direct impact on the decisions of firms about green and conventional investment.

Firms invest in conventional and green capital by using retained profits, loans and bonds. Commercial banks accumulate capital and distribute part of their profits to households. They impose credit rationing on firm loans. This means that they play an active role in the determination of output and the accumulation of green capital. Households receive labour income, buy durable consumption goods and accumulate wealth in the form of deposits, corporate bonds and government securities (there are no household loans). Corporate bonds can be either green or conventional. When the demand for green bonds increases, the price of these bonds tends to go up, leading to a lower cost of borrowing for green projects.

Central banks determine the base interest rate, provide liquidity to the commercial banks and purchase government securities and corporate bonds. Governments collect taxes, decide about the level of government expenditures and can implement bailout programmes if there are financial problems in the banking sector. Inflation has been assumed away and, for simplicity, the price of goods is equal to unity. We use US dollar (\$) as a reference currency.

⁴ A more realistic formulation would be to assume different 'shades of green' depending on the number of 'green' properties that each capital has. In that case the 'greenest' capital would be that capital that can generate renewable energy and is endowed by lower energy intensity, lower material intensity and higher recycling rate compared to conventional capital. On the other hand, the least 'green' capital would be the capital that has only one of these properties. However, such a formulation would complicate the model significantly since it would require the distinction between many types of green investment and would make the calibration of the model a much more challenging exercise.

2.1 Ecosystem

Table 1 depicts the physical flow matrix of our model. This matrix captures the First and the Second Law of Thermodynamics. The First Law of Thermodynamics implies that energy and matter cannot be created or destroyed when they are transformed during the economic processes. This is reflected in the material and energy balance. The first column in Table 1 depicts the material balance in Gigatonnes (Gt).⁵ According to this balance, the total inputs of matter into the socio-economic system over a year (extracted matter, the carbon mass of non-renewable energy and the oxygen included in CO₂ emissions) should be equal to the total outputs of matter over the same year (industrial CO₂ emissions and waste) plus the change in socio-economic stock. The second column in Table 1 depicts the energy balance in Exajoules (EJ). According to this balance, the total inputs of energy into the socio-economic system over a year should be equal to the total outputs of energy over the same year. Symbols with a plus sign denote inputs into the socio-economic system. Symbols with a minus sign denote outputs or changes in socio-economic stock. The Second Law of Thermodynamics is captured by the fact that the economic processes transform low-entropy energy (e.g. fossil fuels) into high-entropy dissipated energy (e.g. thermal energy).

Table 1: Physical flow matrix

	Material balance	Energy balance
Inputs		
Extracted matter	+ M	
Renewable energy		+ ER
Non-renewable energy	+ CEN	+ EN
Oxygen used for fossil fuel combustion	+ $O2$	
Outputs		
Industrial CO ₂ emissions	- $EMIS_{IN}$	
Waste	- W	
Dissipated energy		- ED
Change in socio-economic stock	- ΔSES	
Total	0	0

Note: The table refers to annual global flows. Matter is measured in Gt and energy is measured in EJ.

⁵ For the use of the material balance in material flow accounting, see Fischer-Kowalski et al. (2011).

Table 2 displays the physical stock-flow matrix of our model.⁶ This matrix presents the dynamic change in those physical stocks that are considered more important for human activities. These are the material and non-renewable energy reserves, the atmospheric CO₂ concentration, the socio-economic stock and the stock of hazardous waste. The first row of the matrix shows the stocks of the previous year. The last row presents the stocks at the end of the current year after the additions to stocks and the reductions of stocks have taken place. Additions are denoted by a plus sign. Reductions are denoted by a minus sign.

Table 2: Physical stock-flow matrix

	Material reserves	Non-renewable energy reserves	Atmospheric CO ₂ concentration	Socio-economic stock	Hazardous waste
Opening stock	REV_{M-1}	REV_{E-1}	$CO2_{AT-1}$	SES_{-1}	HWS_{-1}
Additions to stock					
Resources converted into reserves	$+CON_M$	$+CON_E$			
CO ₂ emissions			$+EMIS$		
Production of material goods				$+MY$	
Non-recycled hazardous waste					$+ba\zeta W$
Reductions of stock					
Extraction/use of matter or energy	$-M$	$-EN$			
Net transfer of CO ₂ to oceans/biosphere			$+(\phi_1 - 1)CO2_{AT-1} + \phi_2 CO2_{UP-1}$		
Demolished/disposed socio-economic stock				$-DEM$	
Closing stock	REV_M	REV_E	$CO2_{AT}$	SES	HWS

Note: The table refers to annual global stocks and flows. Matter is measured in Gt and energy is measured in EJ.

The reserves of matter and non-renewable energy are those volumes expected to be produced economically using the existing technology. The reserves stem from the resources which are the volumes presenting technical difficulties, are costly to extract or have not yet been discovered. When resources are converted into reserves, it means that people have a higher stock of matter and energy to rely on for economic processes. Note that although this conversion is important for human activities, it does not represent a physical transformation.

Tables 1 and 2 imply that in our model the laws of thermodynamics are important for three reasons. First, the First Law of Thermodynamics allows us to incorporate explicitly the harmful by-products of energy and matter transformation (CO₂ emissions and hazardous material waste). As will be explained below, these by-products cause the degradation of ecosystem services with feedback effects on the economy. Second, the Second Law of Thermodynamics implies that in the very long run the economic processes cannot rely on the energy produced from fossil fuels. Since the fossil fuel resources are finite and the economic

⁶ For a similar presentation of the physical stock-flow interactions see United Nations (2014).

processes transform the low-entropy energy embodied in these resources into high-entropy energy, sustainability requires the reliance of economic processes on renewable energy sources (even if there was no climate change). Third, by combining the laws of thermodynamics with Georgescu-Roegen's analysis of material degradation, it turns out that recycling might not be sufficient to ensure the availability of the material resources that are necessary for the economic processes. Hence, the depletion of matter needs to be checked separately.

We proceed to describe the equations of the model that refer to the ecosystem.

2.1.1 Matter, recycling and waste

The goods produced every year, denoted by Y , embody a specific amount of matter, MY (Eq. 1).⁷ Material intensity (μ) is defined as the matter included in each output produced. The socio-economic stock (SES) is the material content of the capital goods (K) and durable consumption goods (DC) that remain in the socio-economic system. Thus, $SES = \mu(K + DC)$. As shown in Eq. (2), the matter embodied in goods comes from extraction (M denotes the extracted matter that is used every year in the production of goods) and the demolished/discarded socio-economic stock that is recycled (REC). The latter is defined in Eq. (3); ρ denotes the recycling rate, which is defined as the ratio of recycled matter to the total amount of demolished/discarded socio-economic stock (DEM). The demolished/discarded socio-economic stock is equal to the material content of the depreciated capital goods and the end-of-life durable consumption goods (Eq. 4); δ is the depreciation rate of capital goods and ξ is the proportion of durable consumption goods discarded every year. Eq. (5) shows that socio-economic stock (SES) increases as a result of the production of new goods and decreases due to the demolition/discard of old material goods.

Eq. (6) reflects the material balance depicted in Table 1. The waste (W) generated during the production process is used as a residual. Regarding non-renewable energy, only its carbon mass, CEN , has been included as input in the material balance. As shown in Eq. (7), this mass is estimated from the industrial emissions ($EMIS_N$) by using the conversion rate of Gt of carbon into Gt of CO_2 (car). Carbon exits the socio-economic system in the form of CO_2 emissions. Oxygen ($O2$) is introduced as an input in the material balance because it is

⁷ For simplicity, we have assumed away the material content of the goods related with government spending (G).

necessary in the fossil fuel combustion process. Eq. (8) gives the mass of the oxygen that is part of the CO₂ emissions. Note that by combining Eqs. (2), (5), (6) and (8) it can be easily shown that $W = DEM - REC$; in other words, the waste is equal to the demolished/discarded socio-economic stock that is not recycled.

Only a small proportion (*haz*) of the waste produced every year is hazardous, i.e. it is harmful to human health or the environment.⁸ This hazardous waste is added to the accumulated stock of hazardous waste, *HWS* (Eq. 9). Eq. (10) defines the per capital accumulated hazardous waste (*hazratio*) which is equal to the accumulated stock of hazardous waste in Gt divided by the population (*POP*).

$$MY = \mu(Y - G) \quad (1)$$

$$M = MY - REC \quad (2)$$

$$REC = \rho DEM \quad (3)$$

$$DEM = \mu(\delta K_{-1} + \xi DC_{-1}) \quad (4)$$

$$SES = SES_{-1} + MY - DEM \quad (5)$$

$$W = M + CEN + O2 - EMIS_{IN} - \Delta SES \quad (6)$$

$$CEN = \frac{EMIS_{IN}}{car} \quad (7)$$

$$O2 = EMIS_{IN} - CEN \quad (8)$$

$$HWS = HWS_{-1} + hazW \quad (9)$$

$$hazratio = \frac{HWS}{POP} \quad (10)$$

The material stock-flow dynamics are presented in Eqs. (11)-(14). Eq. (11) shows that the material reserves (REV_M) decline when matter is extracted (in order to be used in the production of goods) and increase when resources are converted into reserves. The annual conversion (CON_M) is given by Eq. (12). An exogenous conversion rate, denoted by con_M , has been assumed. Eq. (13) describes the change in material resources (RES_M). To capture the scarcity of matter we define the matter depletion ratio (dep_M), which is the ratio of matter that is extracted every year relative to the remaining material reserves (Eq. 14). The higher this ratio the greater the matter depletion problems.

⁸ Asbestos, heavy metals and fluoride compounds are examples of hazardous waste. For an analysis of hazardous waste and its impact on health and the environment see Misra and Pandey (2005).

$$REV_M = REV_{M-1} + CON_M - M \quad (11)$$

$$CON_M = con_M RES_{M-1} \quad (12)$$

$$RES_M = RES_{M-1} - CON_M \quad (13)$$

$$dep_M = \frac{M}{REV_{M-1}} \quad (14)$$

2.1.2 Energy

The energy required for production (E) is a function of output (Eq. 15). When energy intensity (ε) declines, the energy required per unit of output becomes lower. As shown in Eqs. (16) and (17), energy is generated either from renewable (ER) or non-renewable sources (EN). The share of renewable energy in total energy is denoted by θ . The dissipated energy (ED) is determined based on the energy balance (Eq. 18).

$$E = \varepsilon Y \quad (15)$$

$$ER = \theta E \quad (16)$$

$$EN = E - ER \quad (17)$$

$$ED = EN + ER \quad (18)$$

Eqs. (19)-(22) represent the stock-flow dynamics of the energy produced from non-renewables. Eq. (19) shows the change in the non-renewable energy reserves (REV_E). CON_E denotes the amount of resources converted into reserves every year. This amount is determined by Eq. (20), where con_E is the conversion rate. The resources of non-renewable energy (RES_E) change every year according to Eq. (21). The energy depletion ratio (dep_E), which captures scarcity problems, shows the non-renewable energy that is extracted and is used every year, relative to the remaining reserves (Eq. 22).

$$REV_E = REV_{E-1} + CON_E - EN \quad (19)$$

$$CON_E = con_E RES_{E-1} \quad (20)$$

$$RES_E = RES_{E-1} - CON_E \quad (21)$$

$$dep_E = \frac{EN}{REV_{E-1}} \quad (22)$$

2.1.3 Emissions and climate change

Our formalisation of emissions and climate change follows closely the traditional integrated assessment models (see Nordhaus and Sztorc, 2013). Every year industrial CO₂ emissions ($EMIS_{IN}$) are generated due to the use of the non-renewable energy sources (Eq. 23). CO₂ intensity (ω) is defined as the industrial emissions produced per unit of non-renewable energy. Every year land-use CO₂ emissions ($EMIS_L$) are also generated because of changes in the use of land (Eq. 24). These emissions are assumed to decline exogenously at a rate lr . Eq. (25) gives the total emissions ($EMIS$).

The atmospheric CO₂ concentration ($CO2_{AT}$) is driven by these emissions and the carbon cycle. The carbon cycle, represented by Eqs. (26)-(28), shows that every year there is exchange of carbon between the atmosphere and the upper ocean/biosphere and between the upper ocean/biosphere and the lower ocean; $CO2_{UP}$ is the upper ocean/biosphere CO₂ concentration and $CO2_{LO}$ is the lower ocean CO₂ concentration. The higher the net transfers of carbon from the atmosphere into the other two reservoirs the lower the atmospheric CO₂ concentration. The accumulation of atmospheric CO₂ and other greenhouse gases increases radiative forcing, F (Eq. 29), placing upward pressures on the atmospheric temperature, T_{AT} (Eq. 31). $F_{2 \times CO_2}$ is the increase in radiative forcing (since the pre-industrial period) due to doubling of CO₂ concentration from pre-industrial levels ($CO2_{AT-PRE}$) and S is the equilibrium climate sensitivity. For simplicity, the radiative forcing due to non-CO₂ greenhouse gas emissions (F_{EX}) is determined exogenously (Eq. 30).⁹ Eq. (32) shows the change in the temperature of the lower ocean (T_{LO}).

$$EMIS_{IN} = \omega EN \quad (23)$$

$$EMIS_L = EMIS_{L-1}(1-lr) \quad (24)$$

$$EMIS = EMIS_{IN} + EMIS_L \quad (25)$$

$$CO2_{AT} = EMIS + \phi_1 CO2_{AT-1} + \phi_2 CO2_{UP-1} \quad (26)$$

$$CO2_{UP} = \phi_{12} CO2_{AT-1} + \phi_{22} CO2_{UP-1} + \phi_{32} CO2_{LO-1} \quad (27)$$

$$CO2_{LO} = \phi_{23} CO2_{UP-1} + \phi_{33} CO2_{LO-1} \quad (28)$$

$$F = F_{2 \times CO_2} \log_2 \frac{CO2_{AT}}{CO2_{AT-PRE}} + F_{EX} \quad (29)$$

$$F_{EX} = F_{EX-1} + fe_x \quad (30)$$

⁹ For the modelling of radiative forcing as an endogenous function of some key non-CO₂ greenhouse gas emissions, see e.g. Anthoff and Tol (2014).

$$T_{AT} = T_{AT-1} + t_1 \left(F - \frac{F_2 \times CO_2}{S} T_{AT-1} - t_2 (T_{AT-1} - T_{LO-1}) \right) \quad (31)$$

$$T_{LO} = T_{LO-1} + t_3 (T_{AT-1} - T_{LO-1}) \quad (32)$$

2.1.4 Ecological efficiency and technology

The ecological efficiency of production is considered to be higher the lower is the energy, material and CO₂ intensity and the higher is the recycling rate. Ecological efficiency also increases when the share of renewable energy in total energy goes up. CO₂ intensity changes in an exogenous way. As shown in Eqs. (33) and (34), CO₂ intensity is reduced with a declining rate ($g_\omega < 0$ and $\zeta_1 > 0$).¹⁰ This reduction is, for example, related to use of technologies, like carbon capture and storage, and the replacement of coal with other fossil fuels that generate less carbon emissions.

Since, as mentioned above, green capital is characterised by lower material and energy intensity and by higher recycling rate and share of renewable in total energy, the efficiency related to these indicators increases when the ratio of green capital (K_G) to conventional capital (K_C) rises. This is shown in Eqs. (35)-(38). μ , ρ , ε and θ denote, respectively, the material intensity, recycling rate, energy intensity and the share of renewable energy in total energy. ε^{\min} and μ^{\min} are the minimum potential values of energy intensity and material intensity respectively. These minimum values are approached when green capital becomes sufficiently high compared to conventional capital. ρ^{\max} is the maximum potential value of recycling rate which is also approached when K_G/K_C becomes sufficiently high. ε^{\max} , μ^{\max} are, respectively, the maximum potential values of energy intensity and material intensity which are approached when green capital is equal to zero.

The use of logistic functions in Eqs. (35)-(38) allows us to take into account the processes of learning-by-doing and learning-by-installing which play a key role in the diffusion of new technologies.¹¹ It also allows us to derive patterns about the future trajectories of energy intensity and renewable energy that are similar with those of other studies that examine the

¹⁰ See Nordhaus and Sztorc (2013) for a similar assumption.

¹¹ For the importance of these processes in energy systems and renewable energy technologies, see e.g. Kahouli-Brahmi (2009) and Tang and Popp (2016).

use of energy in the next decades (see, for instance, Jones and Warner, 2016; Peters et al., 2017).

$$\omega = \omega_{-1}(1 + g_{\omega}) \quad (33)$$

$$g_{\omega} = g_{\omega-1}(1 - \zeta_1) \quad (34)$$

$$\mu = \mu^{max} - \frac{\mu^{max} - \mu^{min}}{1 + \pi_1 e^{-\pi_2(K_{G-1}/K_{C-1})}} \quad (35)$$

$$\rho = \frac{\rho^{max}}{1 + \pi_3 e^{-\pi_4(K_{G-1}/K_{C-1})}} \quad (36)$$

$$\varepsilon = \varepsilon^{max} - \frac{\varepsilon^{max} - \varepsilon^{min}}{1 + \pi_5 e^{-\pi_6(K_{G-1}/K_{C-1})}} \quad (37)$$

$$\theta = \frac{1}{1 + \pi_7 e^{-\pi_8(K_{G-1}/K_{C-1})}} \quad (38)$$

2.2 Macroeconomy and financial system

Table 3 and Table 4 portray the transactions flow matrix and the balance sheet matrix of our macroeconomy. The transactions flow matrix shows the transactions that take place between the various sectors of the economy (each row represents a category of transactions). For each sector inflows are denoted by a plus sign and outflows are denoted by a minus sign. The upper part of the matrix shows transactions related to the revenues and expenditures of the various sectors. The bottom part of the matrix indicates changes in financial assets and liabilities that arise from transactions. The columns reflect the budget constraints of the sectors. For households, firms, commercial banks and central banks a distinction is made between current and capital accounts. The current accounts register payments made or received. The capital accounts show how the investment in real and financial assets is funded. At the aggregate level, monetary inflows are equal to monetary outflows.

Table 3: Transactions flow matrix

	Households		Firms		Commercial banks		Government sector	Central banks		Total
	Current	Capital	Current	Capital	Current	Capital		Current	Capital	
Consumption		$-C$	$+C$							0
Government expenditures			$+G$				$-G$			0
Conventional investment			$+I_C$	$-I_C$						0
Green investment			$+I_G$	$-I_G$						0
Household disposable income net of depreciation	$-Y_{HD}$	$+Y_{HD}$								0
Wages	$+mN$		$-mN$							0
Taxes	$-T_H$		$-T_F$				$+T$			0
Firms' profits	$+DP$		$-TP$	$+RP$						0
Commercial banks' profits	$+BP_D$				$-BP$	$+BP_U$				0
Interest on deposits	$+int_{DD,t}$				$-int_{DD,t}$					0
Depreciation of green capital			$-\delta K_{G,t}$	$+\delta K_{G,t}$						0
Depreciation of conventional capital			$-\delta K_{C,t}$	$+\delta K_{C,t}$						0
Interest on conventional loans			$-int_{CL,t}$		$+int_{CL,t}$					0
Interest on green loans			$-int_{GL,t}$		$+int_{GL,t}$					0
Interest on conventional bonds	$+coupon_{Cb_{CH,t}}$		$-coupon_{Cb_{C,t}}$					$+coupon_{Cb_{CCB,t}}$		0
Interest on green bonds	$+coupon_{Gb_{GH,t}}$		$-coupon_{Gb_{G,t}}$					$+coupon_{Gb_{CCB,t}}$		0
Interest on government securities	$+int_{SSEC_{H,t}}$				$+int_{SSEC_{B,t}}$		$-int_{SSEC_{G,t}}$	$+int_{SSEC_{CCB,t}}$		0
Interest on advances					$-int_{AA,t}$			$+int_{AA,t}$		0
Depreciation of durable consumption goods	$-\xi DC_{G,t}$	$+\xi DC_{H,t}$								0
Central bank's profits							$+CBP$	$-CBP$		0
Bailout of banks						$+B_{AIDOUT}$	$-B_{AIDOUT}$			0
Δ deposits		$-\Delta D$				$+\Delta D$				0
Δ conventional loans				$+\Delta L_C$		$-\Delta L_C$				0
Δ green loans				$+\Delta L_G$		$-\Delta L_G$				0
Δ conventional bonds		$\bar{p}_{C-\Delta b_{CH}}$		$+\bar{p}_{C-\Delta b_C}$				$\bar{p}_{C-\Delta b_{CCB}}$		0
Δ green bonds		$\bar{p}_{G-\Delta b_{GH}}$		$+\bar{p}_{G-\Delta b_G}$				$\bar{p}_{G-\Delta b_{CCB}}$		0
Δ government securities		$-\Delta SSEC_H$				$-\Delta SSEC_B$	$+\Delta SSEC_G$	$-\Delta SSEC_{CCB}$		0
Δ advances						$+\Delta A$		$-\Delta A$		0
Δ high-powered money						$-\Delta HPM$		$+\Delta HPM$		0
Defaulted loans				$+DL$		$-DL$				0
Total	0	0	0	0	0	0	0	0	0	0

Note: The table refers to annual global flows in trillion US\$.

Table 4 shows the assets and the liabilities of the sectors. We use a plus sign for the assets and a minus sign for the liabilities. Accounting requires that at the aggregate level financial assets are equal to financial liabilities. Hence, the net worth of the economy is equal to the real assets which include the capital stock of firms and the durable consumption goods of households.

Table 4: Balance sheet matrix

	Households	Firms	Commercial banks	Government sector	Central banks	Total
Conventional capital		$+K_C$				$+K_C$
Green capital		$+K_G$				$+K_G$
Durable consumption goods	$+DC$					$+DC$
Deposits	$+D$		$-D$			0
Conventional loans		$-L_C$	$+L_C$			0
Green loans		$-L_G$	$+L_G$			0
Conventional bonds	$+p_C b_{CH}$	$-p_C b_C$			$+p_C b_{CCB}$	0
Green bonds	$+p_G b_{GH}$	$-p_G b_G$			$+p_G b_{GCB}$	0
Government securities	$+SEC_H$		$+SEC_B$	$-SEC$	$+SEC_{CB}$	0
High-powered money			$+HPM$		$-HPM$	0
Advances			$-A$		$+A$	0
Total (net worth)	$+V_H$	$+V_F$	$+K_B$	$-SEC$	$+V_{CB}$	$+K_C + K_G + DC$

Note: The table refers to annual global flows in trillion US\$.

In the next subsections we present the equations for the macroeconomy and the financial system.

2.2.1 Output determination and damages

We assume a Leontief-type production function that incorporates Georgescu-Roegen's distinction between stock-flow and fund-service resources. The stock-flow resources are matter and non-renewable energy. The fund-service resources are labour and capital.¹² We define four different types of potential output. The matter-determined potential output (Y_M^*) is defined in Eq. (39) and is higher the higher are the material reserves, the higher is the recycled matter and the lower is the material intensity. The energy-determined potential output (Y_E^*) is defined in Eq. (40) and is higher the higher are the non-renewable energy reserves, the lower is the energy intensity and the higher is the share of renewable energy in total energy. The capital-determined potential output (Y_K^*) is defined in Eq. (41) and is higher the higher is the capital stock and the productivity of capital (v). Lastly, the labour-determined potential

¹² We assume away Ricardian land.

output (Y_N^*) is defined in Eq. (42) and is higher the higher is the labour force (LF), the hourly labour productivity (λ) and the annual working hours per employee (h). The overall potential output (Y^*) is the minimum of all these potential outputs (Eq. 43).

In line with the post-Keynesian tradition, actual output (Y) is demand-determined (Eq. 44): it is equal to consumption demand (C) plus investment demand (I) plus government expenditures (G). However, demand is not independent of supply. When actual output approaches potential output, demand tends to decline as a result of supply-side constraints. This is captured by our investment and consumption functions described below. We define four ratios which capture the extent to which potential output is utilised (Eqs. 45-48). The first two ratios are the matter utilisation rate (um) and the energy utilisation rate (ue), which refer to the use of stock-flow resources.¹³ When these ratios increase, the output produced approaches the potential output determined by the material and energy reserves. The last two ratios are the utilisation rate (u) and the rate of employment (re), which refer to the use of fund-service resources. A rise in these ratios reflects a higher scarcity of capital and labour.

$$Y_M^* = \frac{REV_{M-1} + REC}{\mu} \quad (39)$$

$$Y_E^* = \frac{REV_{E-1}}{(1-\theta)\epsilon} \quad (40)$$

$$Y_K^* = vK \quad (41)$$

$$Y_N^* = \lambda h LF \quad (42)$$

$$Y^* = \min(Y_M^*, Y_E^*, Y_K^*, Y_N^*) \quad (43)$$

$$Y = C + I + G \quad (44)$$

$$um = \frac{Y - G}{Y_M^*} \quad (45)$$

$$ue = \frac{Y}{Y_E^*} \quad (46)$$

$$u = \frac{Y}{Y_K^*} \quad (47)$$

$$re = \frac{Y}{Y_N^*} \quad (48)$$

Global warming causes damages to the fund-service resources (capital and labour), reducing thereby the potential output determined by them. There are two types of damages: the

¹³ Recall that we have assumed away the material content of the goods related with government spending.

damages that affect directly the funds (capital stock and labour force) and the damages that affect the productivities of the funds (capital productivity and labour productivity). Capital stock is affected because climate change can destroy infrastructure by causing storms or inundations, or because it can trigger the abandonment of capital in coastal areas by causing a rise in the sea level (see Dietz and Stern, 2015; Naqvi, 2015; Taylor et al., 2016). The proportion of the population that participates in the labour force might decline as a result of global warming. The reason is that climate change has an adverse impact on the health of the population (see e.g. Watts et al., 2017) and poor health reduces labour force participation. Capital productivity can be driven down since climate change might create a hostile environment that can reduce the ability of firms to use capital effectively (Stern, 2013; Dietz and Stern, 2015). Finally, by affecting the health of the workers, the conditions in workplaces and the accumulation of knowledge, climate change might decrease the ability of people to perform work tasks, reducing labour productivity (Kjellstrom et al., 2009; Dell et al., 2014; Dietz and Stern, 2015; Taylor et al., 2016).

Aggregate demand is affected by these damages in two ways. First, the catastrophes caused by climate change might increase the fears of entrepreneurs that their capital will be destroyed or that it will have very low returns. This reduces their desired investment.¹⁴ Moreover, experiencing or observing the natural disasters and the health problems, households might be induced to save more for precautionary reasons.¹⁵ This can lead to less consumption. Measures that restrict consumption directly might also be adopted as climate damages become more significant. Second, since global warming damages tend to reduce Y_K^* and Y_N^* , they place upward pressures on u and re . As mentioned above, this rise in the scarcity of capital and labour can reduce consumption and investment demand.

Importantly, societies do not react passively to the climate change-related effects on fund-service resources. They take adaptation measures that limit global warming damages. Drawing on de Bruin et al. (2009), we thereby make a distinction between gross damages and net damages. Gross damages are the initial damages caused by climate change if there were no

¹⁴ Taylor et al. (2016) have postulated a negative impact of climate change on investment demand by assuming that greenhouse gas concentration reduces the profit share.

¹⁵ For some empirical evidence about the impact of natural disasters on the saving behaviour of households, see Skidmore (2001).

adaptation measures and net damages are the damages that remain after the implementation of adaptation measures.¹⁶

Eq. (49) is the damage function, which shows how atmospheric temperature and damages are linked. D_T is the proportional gross damage which lies between 0 (no damage) and 1 (complete catastrophe). The form of Eq. (49) has been suggested by Weitzman (2012), who argues that the quadratic forms of damage functions used in the traditional literature of integrated assessment models do not adequately capture high-temperature damages. This issue is tackled by inserting the term $\eta_3 T_{AT}^{6.754}$ where η_3 and the corresponding exponent have been selected such that $D_T = 0.5$ when $T_{AT} = 6^\circ\text{C}$.

In most integrated assessments models D_T affects directly the supply-determined output. On the contrary, as mentioned above, in our model D_T affects the potential output and the aggregate demand. Hence, the variable D_T enters into both (i) the determination of funds and their productivities (see Eqs. 73, 74, 77 and 116) and (ii) the consumption and investment demand (see Eqs. 57 and 102). It is also necessary to partition the gross damage between the fund (D_{TF}) and its productivity (D_{TP}), so as to warrant that when $D_T = x\%$ the capital-determined potential output and the labour-determined potential output would be reduced by $x\%$ if there were no adaptation measures. This is done by Eqs. (50) and (51).¹⁷

The impact of adaptation is captured by the parameters ad_P , ad_K and ad_{LF} that represent the proportion of the gross damage (of productivity, capital stock and labour force respectively) which is eliminated due to adaptation measures. We have that $0 \leq ad_P, ad_K, ad_{LF} \leq 1$. This means that, for example, the proportional net damage to productivity is given by $(1 - ad_P)D_{TP}$. We assume that adaptation does not affect investment and consumption demand: firms and households make decisions based on gross damages.

$$D_T = 1 - \frac{1}{1 + \eta_1 T_{AT} + \eta_2 T_{AT}^2 + \eta_3 T_{AT}^{6.754}} \quad (49)$$

$$D_{TP} = p D_T \quad (50)$$

$$D_{TF} = 1 - \frac{1 - D_T}{1 - D_{TP}} \quad (51)$$

¹⁶ We do not include the financial cost of the adaptation measures in net damages.

¹⁷ See also Moyer et al. (2015).

2.2.2 Firms

The total gross profits of firms (TP_G) are given by Eq. (52); w is the wage rate, N is the number of employed workers, int_C is the interest rate on conventional loans, int_G is the interest rate on green loans, $coupon_C$ denotes the coupon payments on conventional bonds, $coupon_G$ denotes the coupon payments on green bonds, L_C is the amount of conventional loans, L_G is the amount of green loans, b_C is the number of conventional bonds, b_G is the number of green bonds and δ is the depreciation of capital stock (which is assumed to be the same for green capital and conventional capital). The net profits of firms (TP) are equal to gross profits minus the taxes on firms' profits (T_F) (Eq. 53). Firms' retained profits (RP) are a proportion (s_F) of their total profits (Eq. 54). The distributed profits of firms (DP) are determined as a residual (Eq. 55). Eq. (56) gives the rate of retained profits (r).

$$TP_G = Y - wN - int_C L_{C-1} - int_G L_{G-1} - \delta K_{-1} - coupon_C b_{C-1} - coupon_G b_{G-1} \quad (52)$$

$$TP = TP_G - T_F \quad (53)$$

$$RP = s_F TP_{-1} \quad (54)$$

$$DP = TP - RP \quad (55)$$

$$r = RP/K \quad (56)$$

Firms' investment is formalised as a two-stage process. At a first stage, firms decide their overall desired investment in both green and conventional capital. At a second stage, they allocate their desired investment between the two types of capital. Eq. (57) captures the first stage. The desired investment (I^D), adjusted for the damage effect, is equal to net investment plus the depreciated capital; α_{00} , α_{01} , α_1 , α_2 , α_{31} , α_{41} and α_{51} are parameters.

Net investment is affected by a number of factors. First, following the Kaleckian approach (see e.g. Blecker, 2002), it depends positively on the rate of (retained) profits (r) and the rate of capacity utilisation (u). The impact of these factors is assumed to be non-linear in general line with the tradition that draws on Kaldor (1940). This means that when the profit rate and capacity utilisation are very low or very high, their effects on investment become rather small.

Second, following Skott and Zipperer (2012), we assume a non-linear impact of the unemployment rate (ur) on investment: when unemployment approaches zero, there is a

scarcity of labour that discourages entrepreneurs to invest. This employment effect captures Marx's and Kalecki's insights, according to which high employment strengthens the power of workers, having an adverse impact on the business climate. Theoretically, this negative effect of employment could be put into question in the presence of immigration and labour-augmenting investment. In the presence of immigration, entrepreneurs can expect that the flow of immigrants will relax the labour shortage constraint. Thus, investment might not decline when employment approaches the full employment level. However, this does not apply in our model, since we analyse the global economy and, thus, there is no immigration effect. Regarding labour-augmenting investment, it could be argued that when entrepreneurs observe an unemployment rate close to zero, they could relax the labour shortage constraint by increasing investment that enhances labour productivity. However, the adverse impact of climate change on labour productivity, that takes place in our model, makes it more difficult for the entrepreneurs to expect that more investment in labour-augmenting technologies would relax the labour shortage constraint. Therefore, in the presence of climate change, it is less likely that firms will try to invest more in order to increase productivity and reduce the employment rate.¹⁸

Third, the scarcity of energy and material resources can dampen investment, for example because of a rise in resource prices; ue and um capture the utilisation of energy and material resources respectively. This impact, however, is highly non-linear: energy and material scarcity affects investment only once the depletion of the resources has become very severe.

Forth, in order to capture exogenous random factors that might affect desired investment, we have assumed that I^D also depends on a random component, ε_I , that follows a stochastic AR(1) process. Overall, our investment function implies that demand declines (or stops increasing) when it approaches potential output. This allows us to take explicit into account the environmental supply-side effects on aggregate demand mentioned above.

The second stage of the investment process is reflected in Eqs. (58)-(62). At this stage firms decide about the proportion, β , of green investment (I_G^D) in the overall desired investment (Eq. 58). Desired conventional investment (I_C^D) is determined as a residual (Eq. 59). The proportion of green investment depends on two factors (Eq. 60). The first factor is captured

¹⁸ Note, though, that our model takes into account the general role of labour-augmenting technologies by using the Kaldor-Verdoorn law in the determination of labour productivity.

by the term $\beta_0 + \beta_1$ which reflects exogenous developments, such as the cost of installing and using green capital relative to conventional capital or institutional/policy changes that promote green investment (such as carbon pricing). It is assumed that β_0 increases every year but with a declining rate (Eqs. 61 and 62). β_1 is constant but can change due to exogenous institutional, technological or policy shocks. The second factor, captured by the term $\beta_2 [sh_{L-1}(int_G - int_C) + (1 - sh_{L-1})(yield_{G-1} - yield_{C-1})]$, reflects the borrowing cost of investing in green capital relative to conventional capital; $yield_C$ is the yield on conventional bonds, $yield_G$ is the yield on green bonds and sh_L is the share of loans in the total liabilities of firms (loans plus bonds). As the cost of borrowing of green capital (via bank lending or bonds) declines compared to conventional capital, firms tend to increase green investment.

As mentioned above, retained profits are not in general sufficient to cover the desired investment expenditures. This means that firms need external finance, which is obtained via bonds and bank loans. It is assumed that firms first issue bonds and then demand new loans from banks in order to cover the rest amount of their desired expenditures. Only a proportion of the demanded new loans is provided.¹⁹ In other words, the model assumes that there is a quantity rationing of credit. This is in line with recent empirical evidence that shows that the quantity rationing of credit is a more important driver of macroeconomic activity than the price rationing of credit (see Jakab and Kumhof, 2015).

Eq. (63) gives the desired new green loans (NL_G^D) and Eq. (64) gives the desired new conventional loans (NL_C^D). The green, conventional and total investment goods after credit rationing are shown in Eqs. (65), (66) and (67); I_G is green investment, I_C is conventional investment, \bar{p}_C is the par value of conventional bonds, \bar{p}_G is the par value of green bonds, DL is the amount of defaulted loans and def is the rate of default. The total loans of firms (L) are equal to conventional loans plus green loans (Eq. 68). The change in green and conventional capital stock is equal to gross investment minus the depreciation of capital (Eqs. 69 and 70). Eq. (71) shows that total capital (K) is equal to conventional capital (K_C) plus green capital (K_G). The ratio of green capital to total capital (κ) is given by Eq. (72).

$$I^D = \left(\frac{\alpha_{00}}{1 + \exp(\alpha_{01} - \alpha_1 u_{-1} - \alpha_2 r_{-1} + \alpha_{31} u r_{-1}^{-\alpha_{32}} + \alpha_{41} (1 - u e_{-1})^{-\alpha_{42}} + \alpha_{51} (1 - u m_{-1})^{-\alpha_{52}})} K_{-1} + \varepsilon_I K_{-1} + \delta K_{-1} \right) (1 - D_{T-1}) \quad (57)$$

¹⁹ See also Dafermos (2012) and Nikolaidi (2014).

$$I_G^D = \beta I^D \quad (58)$$

$$I_C^D = I^D - I_G^D \quad (59)$$

$$\beta = \beta_0 + \beta_1 - \beta_2 [sh_{L-1}(int_G - int_C) + (1 - sh_{L-1})(yield_{G-1} - yield_{C-1})] \quad (60)$$

$$\beta_0 = \beta_{0-1}(1 + g_{\beta 0}) \quad (61)$$

$$g_{\beta 0} = g_{\beta 0-1}(1 - \zeta_2) \quad (62)$$

$$NL_G^D = I_G^D - \beta RP + repL_{G-1} - \delta K_{G-1} - \bar{p}_G \Delta b_G \quad (63)$$

$$NL_C^D = I_C^D - (1 - \beta)RP + repL_{C-1} - \delta K_{C-1} - \bar{p}_C \Delta b_C \quad (64)$$

$$I_G = \beta RP + \Delta L_G + \delta K_{G-1} + \bar{p}_G \Delta b_G + defL_{G-1} \quad (65)$$

$$I_C = RP + \Delta L_C + \Delta L_G + \delta K_{-1} - I_G + \bar{p}_G \Delta b_G + \bar{p}_C \Delta b_C + DL \quad (66)$$

$$I = I_C + I_G \quad (67)$$

$$L = L_C + L_G \quad (68)$$

$$K_G = K_{G-1} + I_G - \delta K_{G-1} \quad (69)$$

$$K_C = K_{C-1} + I_C - \delta K_{C-1} \quad (70)$$

$$K = K_C + K_G \quad (71)$$

$$\kappa = K_G / K \quad (72)$$

Eq. (73) shows the rate of capital depreciation. Interestingly, a higher depreciation due to climate change has two countervailing effects on economic growth. On the one hand, capital-determined potential output is reduced, placing adverse supply-side effects on economic activity (see Eq. 41); in addition, desired investment might go down because depreciation affects the profitability of firms. On the other hand, aggregate demand tends to increase because a higher depreciation leads to higher gross investment (see Eq. 57).

Eqs. (74) and (77) refer to capital and labour productivity respectively. As argued above, both productivities are influenced by climate change. Labour productivity is affected by exogenous technology factors reflected in the term $\sigma_0 + \sigma_1$ (see Eq. 75). These factors increase productivity growth (g_λ) every year but with a declining rate. Also, in line with the Kaldor-Verdoorn law (see Lavoie, 2014, ch. 6), the growth rate of labour productivity is positively affected by the growth rate of output (g_Y). Note that, although a lower labour productivity can reduce the unemployment rate for a given level of output, it has adverse effects on the supply side by driving down the labour-determined potential output (see Eq. 42).

Eq. (78) gives the wage rate. The wage share (s_w) is assumed to be exogenous. The number of employees is determined by Eq. (79). The unemployment rate is defined in Eq. (80).

$$\delta = \delta_0 + (1 - \delta_0)(1 - ad_K)D_{TF-1} \quad (73)$$

$$v = v_{-1}[1 - (1 - ad_P)D_{TP-1}] \quad (74)$$

$$g_\lambda = \sigma_0 + \sigma_1 + \sigma_2 g_{Y-1} \quad (75)$$

$$\sigma_0 = \sigma_{0-1}(1 - \zeta_3) \quad (76)$$

$$\lambda = \lambda_{-1}(1 + g_\lambda)[1 - (1 - ad_P)D_{TP-1}] \quad (77)$$

$$w = s_w \lambda h \quad (78)$$

$$N = \frac{Y}{h\lambda} \quad (79)$$

$$ur = 1 - re \quad (80)$$

For simplicity, the bonds issued by firms are assumed to be one-year coupon bonds.²⁰ Once they have been issued at their par value, their market price and yield are determined according to their demand. Firms set the coupon rate of bonds based on their yield in the previous year. This means that an increase in the market price of bonds compared to their par value causes a decrease in their yield, allowing firms to issue new bonds with a lower coupon rate.

Eqs. (81) and (82) show the proportion of firms' desired investment which is funded via conventional and green bonds respectively; x_1 is the proportion of firms' conventional desired investment financed via bonds, x_2 is the proportion of firms' green desired investment funded via bonds, \bar{p}_C is the par value of conventional bonds and \bar{p}_G is the par value of green bonds. Eqs. (83)-(84) show that the proportion of desired investment covered by green or conventional bonds is a negative function of the bond yield. In other words, firms fund a lower proportion of their investment via bonds when the cost of borrowing increases. Eqs. (85) and (86) show that the growth rate of the proportion of firms' green desired investment funded via bonds ($g_{x_{20}}$) increases with a declining rate ($g_{x_{20}} > 0$ and $\zeta_4 > 0$). This reflects the fact that the green bond market is expected to expand in the next years and firms are likely to use this market more in order to fund their green investment.

²⁰ This assumption, which does not change the essence of the analysis, allows us to abstract from complications that would arise from having firms that accumulate bonds with different maturities.

Eqs. (87) and (88) show the yield of conventional and green bonds, respectively. The yield of bonds is equal to the coupon payments of the bonds divided by their market price. When this yield increases, the coupon payment (for a given par value) goes up. This is captured by Eqs. (89) and (90). Note that the coupon rate is given by the coupon payment divided by the par value. Thus, when the yield increases, the coupon rate increases too. Eqs. (91) and (92) define the value of conventional bonds (B_C) and green bonds (B_G) respectively; B_{CH} is the value of conventional bonds held by households, B_{CCB} is the value of conventional bonds held by central banks, B_{GH} is the value of green bonds held by households and B_{GCB} is the value of green bonds held by central banks. We postulate a price-clearing mechanism in the bond market (see Eqs. 93 and 94). p_C is the market price of conventional bonds and p_G is the market price of green bonds. Eq. (95) shows the value of total bonds (B) that is equal to the value of conventional plus the value of green bonds.

$$b_c = b_{c-1} + \frac{x_1 I_c^p}{\bar{p}_c} \quad (81)$$

$$b_g = b_{g-1} + \frac{x_2 I_g^p}{\bar{p}_g} \quad (82)$$

$$x_1 = x_{10} - x_{11} \text{yield}_{C-1} \quad (83)$$

$$x_2 = x_{20} - x_{21} \text{yield}_{G-1} \quad (84)$$

$$x_{20} = x_{20-1} (1 + g_{x20}) \quad (85)$$

$$g_{x20} = g_{x20-1} (1 - \zeta_4) \quad (86)$$

$$\text{yield}_C = \frac{\text{coupon}_C}{p_C} \quad (87)$$

$$\text{yield}_G = \frac{\text{coupon}_G}{p_G} \quad (88)$$

$$\text{coupon}_C = \text{yield}_{C-1} \bar{p}_C \quad (89)$$

$$\text{coupon}_G = \text{yield}_{G-1} \bar{p}_G \quad (90)$$

$$B_C = B_{CH} + B_{CCB} \quad (91)$$

$$B_G = B_{GH} + B_{GCB} \quad (92)$$

$$p_C = \frac{B_C}{b_C} \quad (93)$$

$$p_G = \frac{B_G}{b_G} \quad (94)$$

$$B = B_C + B_G \quad (95)$$

Firms might default on their loans. When this happens, a part of their accumulated loans is not repaid, deteriorating the financial position of banks. The amount of defaulted loans (DL) is a proportion (def) of total loans of firms (see Eq. 96). The rate of default (def) is assumed to increase when firms become less liquid (see Eq. 97); def^{max} is the maximum default rate and def_0 , def_1 and def_2 are parameters.²¹ This suggests that, as cash outflows increase compared to cash inflows, the ability of firms to repay their debt declines. The illiquidity of firms is captured by an illiquidity ratio, $illiq$, which expresses the cash outflows of firms relative to their cash inflows (see Eq. 98). Cash outflows include wages, interest, taxes, loan repayments and maintenance capital expenditures (which are equal to depreciation). Cash inflows comprise the revenues from sales and the funds obtained from bank loans and the issuance of bonds. CR_C is the degree of credit rationing on conventional loans and CR_G is the degree of credit rationing on green loans. Eq. (99) defines the debt service ratio (dsr), which is the ratio of debt payment commitments (interest plus principal repayments) to profits before interest. Its key difference with the illiquidity ratio is that the latter takes into account the new flow of credit.

$$DL = defL_{-1} \quad (96)$$

$$def = \frac{def^{max}}{1 + def_0 \exp(def_1 - def_2 illiq_{-1})} \quad (97)$$

$$illiq = \frac{(int_C + rep)L_{C-1} + (int_G + rep)L_{G-1} + coupon_C b_{C-1} + coupon_G b_{G-1} + wN + T_F + \delta K_{-1}}{Y + (1 - CR_C)NL_C^D + (1 - CR_G)NL_G^D + p_C \Delta b_C + p_G \Delta b_G} \quad (98)$$

$$dsr = \frac{(int_C + rep)L_{C-1} + (int_G + rep)L_{G-1} + coupon_C b_{C-1} + coupon_G b_{G-1}}{TP + int_C L_{C-1} + int_G L_{G-1} + coupon_C b_{C-1} + coupon_G b_{G-1}} \quad (99)$$

2.2.3 Households

Eq. (100) gives the gross disposable income of households (Y_{HG}); BP_D denotes the distributed profits of banks, int_D is the interest rate on deposits, D is the amount of deposits, int_s is the interest rate on government securities, SEC_H is the amount of government securities held by households, b_{CH} is the number of conventional corporate bonds held by households and b_{GH} is the number of green bonds held by households. Eq. (101) defines the net disposable income of households (Y_H), which is equal to the gross disposable income minus the taxes on households' gross disposable income (T_H). Households' consumption (C_N), adjusted for

²¹ We use a logistic function, in similar lines with Caiani et al. (2016).

global warming damages, depends on lagged income (which is a proxy for the expected one) and lagged financial wealth (Eq. 102). However, Eq. (102) holds only when there are no supply-side constraints; in that case, $C = C_N$. If the overall demand in the economy is higher than the supply-determined output, Y^* , consumption adjusts such that the overall demand in the economy is below Y^* ; note that pr is slightly lower than 1. This is shown in Eq. (103).

$$Y_{HG} = wN + DP + BP_D + int_D D_{-1} + int_S SEC_{H-1} + coupon_C b_{CH-1} + coupon_G b_{GH-1} \quad (100)$$

$$Y_H = Y_{HG} - T_H \quad (101)$$

$$C_N = (c_1 Y_{H-1} + c_2 V_{HF-1})(1 - D_{T-1}) \quad (102)$$

$$C = C_N \text{ if } C_N + I + G < Y^*; \text{ otherwise } C = pr(Y^* - G - I) \quad (103)$$

Eq. (104) defines the financial wealth of households (V_{HF}). Households invest their expected financial wealth in four different assets: government securities (SEC_H), conventional corporate bonds (B_{CH}), green corporate bonds (B_{GH}) and deposits (D). In the portfolio choice, captured by Eqs. (105)-(108n), Godley's (1999) imperfect asset substitutability framework is adopted.²²

Households' asset allocation is driven by three factors. The first factor is the global warming damages. We posit that damages affect households' confidence and increase the precautionary demand for more liquid and less risky assets (see also Batten et al., 2016). Since damages destroy capital and the profitability opportunities of firms, we assume that as D_T increases, households reduce their holding of corporate conventional bonds and increase the proportion of their wealth held in deposits and government securities which are considered safer.²³ Second, asset allocation responds to alterations in the relative rates on return. The holding of each asset relies positively on its own rate of return and negatively on the other assets' rate of return. Third, a rise in the transactions demand for money (as a result of higher expected income) induces households to substitute deposits for other assets.²⁴

²² The parameters in the portfolio choice equations satisfy the horizontal, vertical and symmetry constraints.

²³ It could be argued that the demand for green corporate bonds is also affected negatively by the climate change damages that harm firms' financial position. However, climate change damages might at the same time induce households to hold more green bonds in order to contribute to the restriction of global warming. Hence, the overall impact of damages on the demand of green bonds is ambiguous. For this reason, we assume that $\lambda'_{30} = 0$ in our simulations.

²⁴ Note that balance sheet restrictions require that Eq. (108n) must be replaced by Eq. (108) in the computer simulations.

Eqs. (109) and (110) show that the growth rate of households' portfolio choice parameter (λ_{30}) related to the autonomous demand for green bonds ($g_{\lambda_{30}}$) increases with a declining rate ($g_{\lambda_{30}} > 0$ and $\zeta_4 > 0$). This captures the fact that the preference for green bonds is expected to increase in the next years. Eq. (111) and (112) show the number of conventional and green bonds held by households.

Recall that all consumption goods in our economy are durable (i.e. they have a life higher than one year). Every year the stock of durable goods increases due to the production of new consumption goods and decreases due to the discard of the accumulated durable goods (Eq. 113).

$$V_{HF} = V_{HF-1} + Y_H - C + b_{CH-1}\Delta p_C + b_{GH-1}\Delta p_G \quad (104)$$

$$\frac{SEC_H}{V_{HF-1}} = \lambda_{10} + \lambda'_{10} D_{T-1} + \lambda_{11} int_S + \lambda_{12} yield_{C-1} + \lambda_{13} yield_{G-1} + \lambda_{14} int_D + \lambda_{15} \frac{Y_{H-1}}{V_{HF-1}} \quad (105)$$

$$\frac{B_{CH}}{V_{HF-1}} = \lambda_{20} + \lambda'_{20} D_{T-1} + \lambda_{21} int_S + \lambda_{22} yield_{C-1} + \lambda_{23} yield_{G-1} + \lambda_{24} int_D + \lambda_{25} \frac{Y_{H-1}}{V_{HF-1}} \quad (106)$$

$$\frac{B_{GH}}{V_{HF-1}} = \lambda_{30} + \lambda'_{30} D_{T-1} + \lambda_{31} int_S + \lambda_{32} yield_{C-1} + \lambda_{33} yield_{G-1} + \lambda_{34} int_D + \lambda_{35} \frac{Y_{H-1}}{V_{HF-1}} \quad (107)$$

$$\frac{D}{V_{HF-1}} = \lambda_{40} + \lambda'_{40} D_{T-1} + \lambda_{41} int_S + \lambda_{42} yield_{C-1} + \lambda_{43} yield_{G-1} + \lambda_{44} int_D + \lambda_{45} \frac{Y_{H-1}}{V_{HF-1}} \quad (108n)$$

$$D = D_{-1} + Y_H - C - \Delta SEC_H - \bar{p}_C \Delta b_{CH} - \bar{p}_G \Delta b_{GH} \quad (108)$$

$$\lambda_{30} = \lambda_{30-1}(1 + g_{\lambda_{30}}) \quad (109)$$

$$g_{\lambda_{30}} = g_{\lambda_{30-1}}(1 - \zeta_4) \quad (110)$$

$$b_{CH} = \frac{B_{CH}}{p_C} \quad (111)$$

$$b_{GH} = \frac{B_{GH}}{p_G} \quad (112)$$

$$DC = DC_{-1} + C - \xi DC_{-1} \quad (113)$$

Eqs. (114) and (115) show that the growth rate of population (g_{POP}) increases with a declining rate ($g_{POP} > 0$ and $\zeta_5 > 0$), reflecting the projections of United Nations (2017). As mentioned above, climate change reduces the ratio labour force to population ratio (Eq. 116). However, there are two additional factors that drive the change in labour force. First, in line with the population projections of United Nations (2017), there are some fundamental dynamics that influence fertility and mortality and tend to reduce the labour force to population ratio. This is reflected in the term lf_i (see Eq. 117). Second, the accumulation of hazardous waste creates

health problems (for instance, carcinogenesis and congenital anomalies) that affect the proportion of the population that is able to work ($\zeta_6 > 0$).

$$g_{POP} = g_{POP-1}(1 - \zeta_5) \quad (114)$$

$$POP = POP-1(1 + g_{POP}) \quad (115)$$

$$LF = (lf_1 - lf_2 \text{hazratio}_{-1})(1 - (1 - ad_{LF})D_{TF-1})POP \quad (116)$$

$$lf_i = lf_{i-1}(1 - \zeta_6) \quad (117)$$

2.2.4 Commercial banks

The profits of banks (BP) are equal to the interest on both conventional and green loans plus the interest on government bonds minus the sum of the interest on deposits and the interest on advances (Eq. 118); SEC_B stands for the government securities that banks hold, int_A is the interest rate on advances and A is the advances. As shown in Eq. (119), the change in the capital of banks (K_B) is equal to their undistributed profits (BP_U) minus the amount of defaulted loans plus the amount of bailout of the government ($BALLOUT$). The undistributed profits of banks are a proportion (s_B) of total profits of banks (see Eq. 120). The distributed profits of banks are determined as the residual (see Eq. 121). According to Eqs. (122) and (123), high-powered money (HPM) and the government securities held by banks are a proportion of deposits. Advances are determined as a residual from the budget constraint of banks (see Eq. 124).²⁵

$$BP = int_C LC_{-1} + int_G LG_{-1} + int_S SEC_{B-1} - int_D D_{-1} - int_A A_{-1} \quad (118)$$

$$K_B = K_{B-1} + BP_U - DL + BALLOUT \quad (119)$$

$$BP_U = s_B BP_{-1} \quad (120)$$

$$BP_D = BP - BP_U \quad (121)$$

$$HPM = h_1 D \quad (122)$$

$$SEC_B = h_2 D \quad (123)$$

$$A = A_{-1} + \Delta HPM + \Delta LG + \Delta LC + \Delta SEC_B + DL - \Delta D - BP_U - BALLOUT \quad (124)$$

As mentioned above, banks impose credit rationing on the loans demanded by firms: they supply only a proportion of demanded loans. Following the empirical evidence presented in

²⁵ Note that if the amount of advances turns out to be negative, the role of residual is played by the government securities.

Lown and Morgan (2006), the degree of credit rationing both on conventional loans (CR_C) and green loans (CR_G) relies on the financial health of both firms and banks (see Eqs. 125 and 126). In particular, credit rationing increases as the debt service ratio of firms (dsr) increases, as the bank leverage (lev_B) increases relative to its maximum acceptable value (lev_B^{max}) and as the capital adequacy ratio (CAR) decreases compared to its minimum acceptable value (CAR^{min}). As in the case of investment, we assume that credit rationing is also dependent on a random component, ε_{CR} , that follows a stochastic AR(1) process; CR^{max} is the maximum degree of credit rationing. Note that $r_0, r_1, r_2, r_3, r_4, l_0, l_1, l_2, l_3$ and l_4 are parameters.

The conventional loans and green loans are defined in Eqs. (127) and (128). Eq. (129) and (130) show the bank leverage ratio and the capital adequacy ratio of banks; w_L and w_S are the risk weights on loans and securities respectively. We assume that when the bank leverage ratio becomes higher than its maximum value and/or the capital adequacy ratio falls below its minimum value, the government steps in and bailouts the banking sector in order to avoid a financial collapse. The bailout takes the form of a capital transfer. This means that it has a negative impact on the fiscal balance and the government acquires no financial assets as a result of its intervention (see Popoyan et al., 2017 for a similar assumption). The bailout funds are equal to the amount that is necessary for the banking sector to restore the capital needed in order to comply with the regulatory requirements.

$$CR_C = \frac{CR^{max}}{1 + r_0 \exp(r_1 - r_2 dsr_{-1} - r_3 (lev_{B-1} - lev_B^{max}) + r_4 (CAR_{-1} - CAR^{min}))} + \varepsilon_{CR} \quad (125)$$

$$CR_G = \frac{CR^{max}}{1 + l_0 \exp(l_1 - l_2 dsr_{-1} - l_3 (lev_{B-1} - lev_B^{max}) + l_4 (CAR_{-1} - CAR^{min}))} + \varepsilon_{CR} \quad (126)$$

$$L_C = L_{C-1} + (1 - CR_C)NL_C^D - repL_{C-1} - defL_{C-1} \quad (127)$$

$$L_G = L_{G-1} + (1 - CR_G)NL_G^D - repL_{G-1} - defL_{G-1} \quad (128)$$

$$lev_B = (L_C + L_G + SEC_B + HPM) / K_B \quad (129)$$

$$CAR = K_B / [w_L(L_C + L_G) + w_S SEC_B] \quad (130)$$

2.2.5 Government sector

The government sector issues securities (SEC) in order to fund its deficit (Eq. 131). The government debt is therefore equal to the accumulated amount of securities. The revenues of the government are equal to taxes (T) plus the central bank profits (CBP). The total spending

of the government consists of government expenditures that are used to buy goods produced by the private sector, the interest on debt and the amount of money used for the bailout of banks. Government expenditures grow at an exogenous rate (gov) (see Eq. 132). The taxes on households' disposable income are a proportion (τ_H) of the gross disposable income (see Eq. 133) and the taxes on firms' profits are a proportion (τ_F) of total gross profits (see Eq. 134). The total taxes are equal to the sum of taxes on households and the taxes on firms (see Eq. 135).

$$SEC = SEC_{-1} + G - T + int_S SEC_{-1} - CBP + BAILOUT \quad (131)$$

$$G = govY_{-1} \quad (132)$$

$$T_H = \tau_H Y_{HG-1} \quad (133)$$

$$T_F = \tau_F TP_{G-1} \quad (134)$$

$$T = T_H + T_F \quad (135)$$

2.2.6 Central banks

Central banks determine the base interest rate, provide liquidity to commercial banks (via advances) and buy government securities (acting as residual purchasers). Moreover, in the context of quantitative easing (QE) programmes, they buy bonds issued by the firm sector.²⁶ Currently, central banks do not explicitly distinguish between the holdings of conventional and green bonds. However, in order to analyse the implications of a green QE programme, we assume that central banks announce separately the amount of conventional bond and green bond purchases.

Nonetheless, the implementation of a green QE programme should not be viewed as a simple extension of the current corporate sector purchase programme of central banks. The current corporate QE programmes have as an aim to improve credit conditions in order to help central banks achieve their inflation targets and they are meant to be of temporary nature. On

²⁶ These bonds are bought on the primary market (the essence of our analysis does not change if we also consider purchases on the secondary market). The purchase of corporate bonds by central banks leads to a temporary increase in the deposits of firms, which is matched by an increase in the excess reserves of commercial banks; the latter are used as intermediaries for the transactions between firms and the central bank. However, firms use all these deposits in order to fund their investment. This means that excess reserves do not appear on the end-of-period balance sheet of commercial banks. Moreover, an implicit assumption that is made is that the temporary increase in the excess reserves of banks does not disrupt the ability of central banks to control the base interest rate, for example because there is a corridor or a floor system in place (for the role of these systems in central bank interest rate setting, see Lavoie, 2014, ch. 4).

the contrary, a green QE would be a kind of industrial policy with a much longer-term commitment. Hence, the decision of central banks to conduct such a programme would require a re-consideration of their mandate or a different interpretation of their role in ensuring financial stability in economies that might face increasing climate-related financial risks. This is especially the case for the central banks of high-income countries, which have narrower mandates and a more strictly defined role in comparison with the central banks of low-income countries (see Campiglio et al., 2018).

The profits of the central bank are defined in Eq. (136); b_{CCB} is the number of conventional corporate bonds held by central banks, b_{GCB} is the number of green bonds held by central banks and SEC_{CB} are the government securities held by central banks.

The value of green corporate bonds held by central banks (B_{GCB}) is a share (s_G) of total outstanding green bonds (see Eq. 137). We assume that this share is currently equal to zero since central banks do not implement green QE programmes. The value of conventional corporate bonds held by central banks (B_{CCB}) is a share (s_C) of total outstanding conventional bonds (see Eq. 138). Currently, this share is very low since the corporate bond purchases of central banks represent a very small proportion of the total bond market.

Eqs. (139) and (140) define the number of conventional corporate bonds held by central banks and the number of green bonds held by central banks respectively. Eq. (141) shows the government securities held by central banks. Eq. (142-red) reflects the capital account of banks and is the redundant equation of the system described in Table 3 and Table 4: it is logically implied by all the other equations of this system.

$$CBP = coupon_C b_{CCB-1} + coupon_G b_{GCB-1} + int_A A_{-1} + int_S SEC_{CB-1} \quad (136)$$

$$B_{GCB} = s_G B_{G-1} \quad (137)$$

$$B_{CCB} = s_C B_{C-1} \quad (138)$$

$$b_{CCB} = \frac{B_{CCB}}{p_C} \quad (139)$$

$$b_{GCB} = \frac{B_{GCB}}{p_G} \quad (140)$$

$$SEC_{CB} = SEC - SEC_H - SEC_B \quad (141)$$

$$SEC_{CB} = SEC_{CB-1} + \Delta HPM - \Delta A - \bar{p}_C \Delta b_{CCB} - \bar{p}_G \Delta b_{GGB} \quad (142\text{-red})$$

3. Baseline scenario

Our baseline scenario represents a ‘business as usual’ pathway whereby the global economy continues to expand in broad line with recent trends, and ecological efficiency improves moderately due to the continuation of technological changes and the implementation of some policies that promote green investment. Some key features of our baseline scenario are shown in Table 5. It is assumed that the economy grows on average at a rate slightly lower than 2.7% till 2050; in other words, we postulate an economic expansion a little bit lower than the one observed over the last two decades or so.²⁷ The unemployment rate remains, on average, close to 6% till 2050. Drawing on the United Nations (2017) population projections (medium fertility variant), the population is assumed to grow at a declining rate, becoming equal to around 9.77bn people in 2050. Moreover, the default rate on corporate loans is assumed to remain, on average, close to its current level, which is slightly higher than 4%.

Table 5: Key features of the baseline scenario

Variable	Value/trend
Economic growth till 2050	slightly lower than 2.7% (on average)
Unemployment rate till 2050	slightly lower than 6% (on average)
Population in 2050	9.77bn
Labour force-to-population ratio in 2050	0.45
Default rate till 2050	slightly higher than 4% (on average)
CO ₂ intensity in 2050 as a ratio of CO ₂ intensity in 2016	around 0.9
Share of renewable energy in total energy in 2050	around 25%
Material intensity in 2050 as a ratio of material intensity in 2016	around 0.9
Energy intensity in 2050 as a ratio of energy intensity in 2016	around 0.7
Recycling rate in 2050 as a ratio of recycling rate in 2016	around 1.4
Annual green investment in the period 2016-2040	around US\$1.1tn
Energy use in 2040 as a ratio of energy use in 2016	around 1.4
Yield of conventional bonds	quite stable till around 2050
Yield of green bonds	declines slightly in the next decade or so

CO₂ intensity (which captures the industrial emissions per unit of fossil-fuel energy) declines by 10% till 2050, for example due to the continuation in the replacement of coal with gas and the use of carbon capture and storage technologies.²⁸ The share of renewable energy increases to about 25% till 2050 (from about 14% which is the current level), while energy intensity is assumed to become approximately 30% lower in 2050 compared to its 2016 level. Material

²⁷ Based on data from World Bank.

²⁸ For the importance of these factors in the determination of CO₂ intensity, see e.g. Peters et al. (2017).

intensity and recycling rate also improve. The overall improvement in ecological efficiency indicators is associated with the accumulation of green capital. In our baseline scenario the annual green investment during the period 2016-2040 is equal to around US\$1.1tn.²⁹ The annual use of energy is 40% higher in 2040 compared to 2016.³⁰

We also assume that the yield on the conventional bond market remains relatively stable till 2050, while the yield of green bonds improves in the next decade or so. The latter is a result of an increasing demand for green bonds that outstrips their supply, in line with recent trends (see, for example, Climate Bonds Initiative, 2017b).

²⁹ Note that IEA (2016, p. 82) estimates that the annual investment in renewables and energy efficiency that is necessary over the period 2016-2040 in order to avoid a global warming higher than 2°C is close to US\$2tn. Recall that green investment in our model does not only include investment in renewables and energy efficiency: it also includes investment that improves material intensity and the recycling rate.

³⁰ In the Current Policies Scenario presented in IEA (2016) the energy use in 2040 is 43% higher compared to 2016.

4. Symbols and values

Table 6: Symbols and initial values for endogenous variables (baseline scenario)

Symbol	Description	Value	Remarks/sources
A	Advances (trillion US\$)	6.8	Calculated from the identity $K_B = L_C + L_G + HPM + SEC_B - A - D$ using the initial values of $K_B, L_C, L_G, HPM, SEC_B$ and D
B	Value of total corporate bonds (trillion US\$)	12.0	Based on OECD (2017, p. 21); we use the figure for the debt securities issued by non-financial corporations
B_{AIIOUT}	Bailout funds provided to the banking system from the government sector	0	No bailout is assumed in 2016 since $lev_B < lev_B^{max}$ and $CAR > CAR^{min}$
B_C	Value of conventional corporate bonds (trillion US\$)	11.8	Calculated from Eq. (95) using the initial values of B and B_G
b_C	Number of conventional corporate bonds (trillions)	0.118	Calculated from Eq. (93) using the initial values of p_C and B_C
B_{CCB}	Value of conventional corporate bonds held by central banks (trillion US\$)	0.1	Based on the recent holdings of central banks as part of their corporate sector purchase programmes
b_{CCB}	Number of conventional corporate bonds held by central banks (trillions)	0.001	Calculated from Eq. (139) using the initial values of p_C and B_{CCB}
B_{CHI}	Value of conventional corporate bonds held by households (trillion US\$)	11.7	Calculated from Eq. (91) using the initial values of B_{CCB} and B_C
b_{CHI}	Number of conventional corporate bonds held by households (trillions)	0.1	Calculated from Eq. (111) using the initial values of p_C and B_{CHI}
B_G	Value of green corporate bonds (trillion US\$)	0.25	Based on Climate Bonds Initiative (2017a); we use the value of the climate-aligned bonds that has been issued by the financial and the non-financial corporate sector
b_G	Number of green corporate bonds (trillions)	0.003	Calculated from Eq. (94) using the initial values of p_G and B_G
B_{GCB}	Value of green corporate bonds held by central banks (trillion US\$)	0	There was no green QE programme in 2016
b_{GCB}	Number of green corporate bonds held by central banks (trillions)	0	Calculated from Eq. (140) using the initial values of p_G and B_{GCB}
B_{GHI}	Value of green corporate bonds held by households (trillion US\$)	0.25	Calculated from Eq. (92) using the initial values of B_G and B_{GCB}
b_{GHI}	Number of green corporate bonds held by households (trillions)	0.0025	Calculated from Eq. (112) using the initial values of p_G and B_{GHI}
BP	Profits of banks (trillion US\$)	3.01	Calculated from Eq. (118) using the initial values of L_C, L_G, SEC_B, D and A
BP_D	Distributed profits of banks (trillion US\$)	0.54	Calculated from Eq. (121) using the initial values of BP and BP_U
BP_U	Retained profits of banks (trillion US\$)	2.47	Calculated from Eq. (120) using the initial value of BP
C	Consumption (trillion US\$)	48.3	No supply-side constraints are assumed in 2016 since $C_N + I + G < Y^*$; therefore $C = C_N$
C_N	Consumption when no supply-side constraints exist (trillion US\$)	48.3	Calculated from Eq. (44) using the initial values of Y, G and I (since $C = C_N$)
CAR	Capital adequacy ratio	0.1	Calculated from Eq. (130) using the initial values of K_B, L_C, L_G and SEC_B
CBP	Central banks' profits (trillion US\$)	0.2	Calculated from Eq. (136) using the initial values of $coupon_C, b_{CCB}, coupon_G, b_{GCB}, A$ and SEC_{CB}
CEN	Carbon mass of the non-renewable energy sources (Gt)	9.9	Calculated from Eq. (7) using the initial value of $EMIS_{IN}$
$CO2_{AT}$	Atmospheric CO ₂ concentration (GtCO ₂)	3146	Taken from NOAA/ESRL (National Oceanic & Atmospheric Administration/Earth System Research Laboratory)
$CO2_{LO}$	Lower ocean CO ₂ concentration (GtCO ₂)	6380.6	Based on the DICE-2016R model (Nordhaus, 2016); GtC have been transformed into GtCO ₂
$CO2_{UP}$	Upper ocean/biosphere CO ₂ concentration (GtCO ₂)	1694.2	Based on the DICE-2016R model (Nordhaus, 2016); GtC have been transformed into GtCO ₂
CON_E	Amount of non-renewable energy resources converted into non-renewable energy reserves (EJ)	1629.0	Calculated from Eq. (20) using the initial value of RES_E
CON_M	Amount of material resources converted into material reserves (Gt)	209	Calculated from Eq. (12) using the initial value of RES_M
$coupon_C$	Fixed coupon paid per conventional corporate bond (US\$)	5	Calculated from Eq. (87) using the initial values of p_C and $yield_C$
$coupon_G$	Fixed coupon paid per green corporate bond (US\$)	5	Calculated from Eq. (88) using the initial values of p_G and $yield_G$
CR_C	Degree of credit rationing for conventional loans	0.2	Calculated from Eq. (125) using the initial values of d_{sr}, lev_B and CAR
CR_G	Degree of credit rationing for green loans	0.3	Calculated from Eq. (126) using the initial values of d_{sr}, lev_B and CAR
D	Deposits (trillion US\$)	65.0	Based on Allianz (2017)
DC	Stock of durable consumption goods (trillion US\$)	1456	Calculated from Eq. (4) using the initial values of K, DEM, δ and μ
def	Rate of default	0.040	Based on World Bank
DEM	Demolished/discarded socio-economic stock (Gt)	17.0	Based on Haas et al. (2015)
dep_E	Energy depletion ratio	0.013	Calculated from Eq. (22) using the initial values of EN and REV_E
dep_M	Matter depletion ratio	0.008	Selected from a reasonable range of values
DL	Amount of defaulted loans (trillion US\$)	2.2	Calculated from Eq. (96) using the initial values of L and def
DP	Distributed profits of firms (trillion US\$)	17.5	Calculated from Eq. (55) using the initial values of TP and RP
d_{sr}	Debt service ratio	0.42	Calculated from Eq. (99) using the initial values of $L_C, L_G, coupon_C, b_C, coupon_G, b_G$ and TP
D_T	Total proportional damage caused by global warming	0.0031	Calculated from Eq. (49) using the initial value of T_{AT}
D_{TF}	Part of damage that affects directly the fund-service resources	0.0028	Calculated from Eq. (51) using the initial values of D_T and D_{TP}
D_{TP}	Part of damage that reduces the productivities of fund-service resources	0.0003	Calculated from Eq. (50) using the initial value of D_T
E	Energy used for the production of output (EJ)	580.0	Based on IEA (International Energy Agency); total primary energy supply is used
ED	Dissipated energy (EJ)	580.0	Calculated from Eq. (18) using the initial values of EN and ER
$EMIS$	Total CO ₂ emissions (GtCO ₂)	38.8	Calculated from Eq. (25) using the initial values of $EMIS_{IN}$ and $EMIS_L$
$EMIS_{IN}$	Industrial CO ₂ emissions (GtCO ₂)	36.2	Taken from CDIAC (Carbon Dioxide Information Analysis Center)
$EMIS_L$	Land-use CO ₂ emissions (GtCO ₂)	2.5	Taken from the DICE-2016R model (Nordhaus, 2016)
EN	Energy produced from non-renewable sources (EJ)	498.8	Calculated from Eq. (17) using the initial values of E and ER
ER	Energy produced from renewable sources (EJ)	81.2	Calculated from Eq. (16) using the initial values of θ and E
F	Radiative forcing over pre-industrial levels (W/m ²)	2.52	Calculated from Eq. (29) using the initial values of $CO2_{AT}$ and F_{EX}
F_{EX}	Radiative forcing, over pre-industrial levels, due to non-CO ₂ greenhouse gases (W/m ²)	0.51	Based on the DICE-2016R model (Nordhaus, 2016)
G	Government expenditures (trillion US\$)	12.5	Calculated from Eq. (132) using the initial value of Y
g_{POP}	Growth rate of population	0.014	Taken from United Nations (medium fertility variant)
g_{s20}	Growth rate of the autonomous proportion of desired green investment funded via bonds	0.040	Calibrated such that the model generates the baseline scenario

(continued from the previous page)

Symbol	Description	Value	Remarks/sources
g_Y	Growth rate of output	0.025	Based on World Bank
g_{30}	Growth rate of the autonomous share of green investment in total investment	0.003	Calibrated such that the model generates the baseline scenario
g_λ	Growth rate of labour productivity	0.012	Calculated from Eq. (75) using the initial values of g_Y and σ_θ
$g_{\lambda 30}$	Growth rate of the households' portfolio choice parameter related to the autonomous demand for green bonds	0.040	Calibrated such that the model generates the baseline scenario
g_ω	Growth rate of CO ₂ intensity	-0.003	Calibrated such that the model generates the baseline scenario
$hazratio$	Hazardous waste accumulation ratio (tonnes per person)	1.87	Calculated from Eq. (10) using the initial values of $HW\bar{S}$ and POP
HPM	High-powered money	13.00	Calculated from Eq. (122) using the initial value of D
$HW\bar{S}$	Stock of hazardous waste (Gt)	14.0	Calculated assuming a constant ratio of hazardous waste to GDP since 1960
I	Total investment (trillion US\$)	15.0	Calibrated such that the model generates the baseline scenario
I_C	Conventional investment (trillion US\$)	14.3	Calculated from Eq. (67) using the initial values of I and I_G
I_C^D	Desired conventional investment (trillion US\$)	16.6	Calculated from the identity $I_C^D = I^D - I_G^D$; we use the initial values of I^D and I_G^D
I^D	Desired total investment (trillion US\$)	17.5	Calibrated such that the model generates the baseline scenario
I_G	Green investment (trillion US\$)	0.7	Based on IEA (2016); we use a higher value than the one reported in IEA (2016) since green investment in our model is not confined to investment in energy efficiency and renewables (it also includes investment in recycling and material efficiency)
I_G^D	Desired green investment (trillion US\$)	0.9	Calculated such that it is reasonably higher than I_G
$illiq$	Illiquidity ratio	0.72	Calculated from Eq. (98) using the initial values of $L_C, L_G, coupon_C, b_C, coupon_G, b_G, w, N, T_F, \delta, K, Y, CR_C, NL_C^D, CR_G, NL_G^D, p_C$ and p_G
K	Total capital stock of firms (trillion US\$)	227.4	Calculated from the identity $K = (K/Y) * Y$ using the initial value of Y and assuming that $K/Y = 3$ (based on Penn World Table 9.0)
K_B	Capital of banks (trillion US\$)	8.4	Calculated from Eq. (129) using the initial values of lev_B, L_C, L_G, SEC_B and HPM
K_C	Conventional capital stock (trillion US\$)	219.0	Calculated from Eq. (71) using the initial values of K and K_G
K_G	Green capital stock (trillion US\$)	8.4	Calculated from Eq. (72) using the initial values of K and α
L	Total loans of firms (trillion US\$)	57.7	Calculated from the identity $L = (credit - B/Y) * Y$; $credit$ is the credit to the non-financial corporations in percent of GDP taken from BIS (Bank for International Settlements); it is assumed that $credit$ includes both loans and bonds
L_C	Conventional loans (trillion US\$)	55.5	Calculated from Eq. (68) using the initial values of L and L_G
L_G	Green loans (trillion US\$)	2.1	Calculated by assuming that $L_G/L = K_G/K = \alpha$; we use the initial values of α and L
lev_B	Banks' leverage ratio	9.6	Taken from World Bank
LF	Labour force (billion people)	3.42	Taken from World Bank
lf_1	Autonomous labour force-to-population ratio	0.460	Calculated from Eq. (116) using the initial values of $LF, POP, hazratio$ and D_{TF}
M	Extraction of new matter from the ground, excluding the matter included in non-renewable energy sources (Gt)	51.5	Taken from UN Environment International Resource Panel Global Material Flows Database; the figure refers to non-metallic minerals plus metal ores
MY	Output in material terms (Gt)	56.6	Calculated from Eq. (2) using the initial values of M and REC
N	Number of employees (billion people)	3.2	Calculated from the definition of the rate of employment ($re = N/LF$) using the initial values of re and LF
NL_C^D	Desired new amount of conventional loans (trillion US\$)	11.1	Calculated from Eq. (64) using the initial values of $I_C^D, \beta, RP, L_C, \delta, K_C$ and b_C
NL_G^D	Desired new amount of green loans (trillion US\$)	0.7	Calculated from Eq. (63) using the initial values of $I_G^D, \beta, RP, L_G, \delta, K_G$ and b_G
O_2	Oxygen used for the combustion of fossil fuels (Gt)	26.3	Calculated from Eq. (8) using the initial values of $EMIS_{DN}$ and CEN
p_C	Market price of conventional corporate bonds (US\$)	100	The price has been normalised such that it is equal to US\$100 (the par value of bonds) in 2016
p_G	Market price of green corporate bonds (US\$)	100	The price has been normalised such that it is equal to US\$100 (the par value of bonds) in 2016
POP	Population (billions)	7.47	Taken from United Nations (medium fertility variant)
r	Rate of retained profits	0.009	Calculated from Eq. (56) using the initial values of RP and K
re	Rate of employment	0.94	Calculated from Eq. (80) using the initial value of re
REC	Recycled socio-economic stock (Gt)	5.1	Calculated from Eq. (3) using the initial values of ρ and DEM
RES_E	Non-renewable energy resources (EJ)	543000	Based on BGR (2016, p. 36)
RES_M	Material resources (Gt)	417245	Calculated by assuming $RES_M/REV_M = 64.8$ (based on UNEP, 2011)
REV_E	Non-renewable energy reserves (EJ)	38000	Based on BGR (2016, p. 36)
REV_M	Material reserves (Gt)	6438	Calculated from Eq. (14) using the initial values of M and dep_M
RP	Retained profits of firms (trillion US\$)	2.0	Calculated from Eq. (54) using the initial value of TP
SEC	Total amount of government securities	63.4	Calculated from the identity $general\ government\ debt\ to\ GDP = SEC/Y$ using the initial value of Y and the value of the $general\ government\ debt\ to\ GDP$ ratio (taken from IMF)
SEC_B	Government securities held by banks (trillion US\$)	9.5	Calculated by assuming that $SEC_B/SEC = 0.2$ based on Alli Abbas et al. (2014)
SEC_{CB}	Government securities held by central banks (trillion US\$)	6.1	Calculated from the identity $SEC_{CB} = HPM + V_{CB} \bar{p}_C b_{CCB} \bar{p}_G b_{CCB} A$ using the initial values of $V_{CB}, b_{CCB}, b_{CCB}, A$ and HPM
SEC_H	Government securities held by households (trillion US\$)	47.7	Calculated from Eq. (141) using the initial values of SEC, SEC_{CB} and SEC_B
SES	Socio-economic stock (Gt)	1506.3	Calculated from the identity $SES = \mu(K + DC)$ using the initial values of μ, K and DC
sh_L	Share of loans in total firm liabilities	0.83	Calculated from the formula $sh_L = L/(L+B)$ using the initial values of L and B
T	Total taxes (trillion US\$)	11.6	Calculated from Eq. (135) using the initial values of T_H and T_F

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Symbol	Description	Value	Remarks/sources
T_{AT}	Atmospheric temperature over pre-industrial levels (°C)	1.04	Based on Met Office
T_F	Taxes on firms' profits (trillion US\$)	3.3	Calculated from Eq. (134) using the initial value of TP_G
T_H	Taxes on households' disposable income	8.2	Calculated from Eq. (133) using the initial value Y_{HG}
T_{LO}	Lower ocean temperature over pre-industrial levels (°C)	0.0112	Based on the DICE-2016R model (Nordhaus, 2016)
TP	Total profits of firms (trillion US\$)	19.5	Calculated from Eq. (53) using the initial values of TP_G and T_F
TP_G	Total gross profits of firms (trillion US\$)	22.9	Calculated from Eq. (52) using the initial values of $Y, w, N, L_C, L_G, \delta, K, coupon_C, b_C, coupon_G$ and b_G
u	Rate of capacity utilisation	0.72	Based on World Bank, Enterprise Surveys
ue	Rate of energy utilisation	0.01	Calculated from Eq. (46) using the initial values of Y and Y_E^*
um	Rate of matter utilisation	0.01	Calculated from Eq. (45) using the initial values of Y, G and Y_M^*
ur	Unemployment rate	0.06	Based on World Bank
v	Capital productivity	0.46	Calculated from Eqs. (41) and (47) using the initial values of Y, u and K
V_{CB}	Wealth of central banks (trillion US\$)	0	It is assumed that there are no accumulated capital gains for the central banks
V_H	Wealth of households (trillion US\$)	1580.6	Calculated from the identity $V_H = DC + D + p_C b_{CH} + p_G b_{GH} + SEC_H$ using the initial values of $SEC_H, p_C, b_{CH}, p_G, b_{GH}, DC$ and D
V_{HF}	Financial wealth of households (trillion US\$)	124.6	Calculated from the identity $V_{HF} = D + p_C b_{CH} + p_G b_{GH} + SEC_H$ using the initial values of $SEC_H, p_C, b_{CH}, p_G, b_{GH}$ and D
w	Annual wage rate (trillion US\$/billions of employees)	12.26	Calculated from Eq. (78) using the initial value of λ
W	Waste (Gt)	11.90	Calculated from the identity $W = DEM - REC$ using the initial values of DEM and REC
x_1	Proportion of desired conventional investment funded via bonds	0.02	Calibrated such that the model generates the baseline scenario
x_2	Proportion of desired green investment funded via bonds	0.01	Calibrated such that the model generates the baseline scenario
x_{20}	Autonomous proportion of desired green investment funded via bonds	0.01	Calculated from Eq. (84) using the initial values of $yield_G$ and x_{20}
Y	Output (trillion US\$)	75.8	Taken from World Bank (current prices)
Y^*	Potential output (trillion US\$)	80.6	Calculated from Eq. (43) using the initial values of Y_M^*, Y_E^*, Y_K^* and Y_N^*
Y_E^*	Energy-determined potential output (trillion US\$)	5774.7	Calculated from Eq. (40) using the initial values of REV_E, θ and ε
Y_H	Disposable income of households (trillion US\$)	51.5	Calculated from Eq. (101) using the initial values of Y_{HG} and T_H
Y_{HD}	Household disposable income net of depreciation (trillion US\$)	57.9	Calculated from the identity $Y_{HD} = Y_H - \delta DC_H$ using the initial values of Y_H and DC
Y_{HG}	Gross disposable income of households (trillion US\$)	59.7	Calculated from Eq. (100) using the initial values of $w, N, DP, BP_D, D, SEC_H, coupon_C, b_{CH}, coupon_G$ and b_{GH}
$yield_C$	Yield on conventional corporate bonds	0.05	Based on FTSE Russell (2016)
$yield_G$	Yield on green corporate bonds	0.05	Based on FTSE Russell (2016)
Y_K^*	Capital-determined potential output (trillion US\$)	105.3	Calculated from Eq. (41) using the initial values of v and K
Y_M^*	Matter-determined potential output (trillion US\$)	7199.9	Calculated from Eq. (39) using the initial values of REV_M, REC and μ
Y_N^*	Labour-determined potential output (trillion US\$)	80.6	Calculated from Eq. (42) using the initial values of λ and LF
β	Share of desired green investment in total investment	0.05	Calculated from Eq. (58) using the initial values of I_G^D and I^D
β_0	Autonomous share of desired green investment in total investment	0.04	Calculated from Eq. (60) using the initial values of $\beta, sb_{L_s}, yield_C$ and $yield_G$
δ	Depreciation rate of capital stock	0.04	Calculated from Eq. (73) using the initial value D_{TF}
ε	Energy intensity (EJ/trillion US\$)	7.65	Calculated from Eq. (15) using the initial values of E and Y
θ	Share of renewable energy in total energy	0.14	Based on IEA (International Energy Agency); total primary energy supply is used
α	Ratio of green capital to total capital	0.04	Selected such that it is reasonably lower than I_G/I
λ	Hourly labour productivity (trillion US\$/ (billions of employees*annual hours worked per employee))	0.01	Calculated from Eq. (79) using the initial values of Y and N
λ_{30}	Households' portfolio choice parameter related to the autonomous demand for green bonds	0.01	Calculated from Eq. (107) using the initial values of $B_{GH}, V_{HF}, D_T, yield_C, yield_G$ and Y_H
μ	Material intensity (kg/\$)	0.89	Calculated from Eq. (1) using the initial values of MY, G and Y
ρ	Recycling rate	0.30	Based on Haas et al. (2015)
σ_0	Autonomous growth rate of labour productivity	-0.02	Calibrated such that the model generates the baseline scenario
ω	CO ₂ intensity of non-renewable energy (GtCO ₂ /EJ)	0.07	Calculated from Eq. (23) using the initial values of $EMIS_{IN}$ and EN

Table 7: Symbols and values for parameters and exogenous variables (baseline scenario)

Symbol	Description	Value	Remarks/sources
ad_K	Fraction of gross damages to capital stock avoided through adaptation	0.80	Selected from a reasonable range of values
ad_{LF}	Fraction of gross damages to labour force avoided through adaptation	0.70	Selected from a reasonable range of values
ad_P	Fraction of gross damages to productivity avoided through adaptation	0.70	Selected from a reasonable range of values
c_1	Propensity to consume out of disposable income	0.65	Calibrated such that the model generates the baseline scenario
c_2	Propensity to consume out of financial wealth	0.13	Empirically estimated using data for a panel of countries over the period 1995-2016 (the econometric estimations are available upon request)
car	Coefficient for the conversion of GtC into GtCO ₂	3.67	Taken from CDIAC (Carbon Dioxide Information Analysis Center)
CAR^{min}	Minimum capital adequacy ratio	0.08	Based on the Basel III regulatory framework
$CO_{2,AT-PRE}$	Pre-industrial CO ₂ concentration in atmosphere (GtCO ₂)	2156.2	Taken from DICE-2016R model (Nordhaus, 2016); GtC have been transformed into GtCO ₂
$CO_{2,LO-PRE}$	Pre-industrial CO ₂ concentration in upper ocean/biosphere (GtCO ₂)	6307.2	Taken from DICE-2016R model (Nordhaus, 2016); GtC have been transformed into GtCO ₂
$CO_{2,UP-PRE}$	Pre-industrial CO ₂ concentration in lower ocean (GtCO ₂)	1320.1	Taken from DICE-2016R model (Nordhaus, 2016); GtC have been transformed into GtCO ₂
con_E	Conversion rate of non-renewable energy resources into reserves	0.003	Selected from a reasonable range of values
con_M	Conversion rate of material resources into reserves	0.0005	Selected from a reasonable range of values
CR^{max}	Maximum degree of credit rationing	0.5	Selected from a reasonable range of values
def^{max}	Maximum default rate of loans	0.2	Selected from a reasonable range of values
def_0	Parameter of the default rate function	4.00	Calculated from Eq. (97) using the initial value of $illiq$
def_1	Parameter of the default rate function	5.65	Calibrated such that the model generates the baseline scenario
def_2	Parameter of the default rate function (related to the sensitivity of the default rate to the illiquidity ratio of firms)	7.81	Selected from a reasonable range of values
F_{2x,CO_2}	Increase in radiative forcing (since the pre-industrial period) due to doubling of CO ₂ concentration from pre-industrial levels (W/m ²)	3.7	Taken from the DICE-2016R model (Nordhaus, 2016)
f_{ex}	Annual increase in radiative forcing (since the pre-industrial period) due to non-CO ₂ agents (W/m ²)	0.006	Based on the DICE-2016R model (Nordhaus, 2016)
gov	Share of government expenditures in output	0.17	Based on World Bank; the figure includes only the consumption government expenditures
h	Annual working hours per employee	1850	Based on Penn World Table 9.0
h_1	Banks' reserve ratio	0.2	Based on World Bank
h_2	Banks' government securities-to-deposits ratio	0.15	Calculated from Eq. (123) using the initial values of SEC_B and D
haz	Proportion of hazardous waste in total waste	0.04	EEA (2012, p. 22) reports a figure equal to 3.7% for EU-27
int_A	Interest rate on advances	0.02	Based on Global Interest Rate Monitor
int_C	Interest rate on conventional loans	0.07	Based on World Bank
int_D	Interest rate on deposits	0.015	Based on World Bank
int_G	Interest rate on green loans	0.08	Based on World Bank; it is assumed that $int_C - int_G = 0.01$
int_S	Interest rate on government securities	0.015	Based on FTSE Russell (2016)
l_0	Parameter of the function of credit rationing on green loans	0.67	Calculated from Eq. (126) using the initial values of dsr , CAR and lev_B
l_1	Parameter of the function of credit rationing on green loans	-0.25	Calibrated such that the model generates the baseline scenario
l_2	Parameter of the function of credit rationing on green loans (related to the sensitivity of credit rationing to the default rate)	2.08	Selected from a reasonable range of values
l_3	Parameter of the function of credit rationing on green loans (related to the sensitivity of credit rationing to the leverage ratio of banks)	0.04	Selected from a reasonable range of values
l_4	Parameter of the function of credit rationing on green loans (related to the sensitivity of credit rationing to the capital adequacy ratio of banks)	2.08	Selected from a reasonable range of values
lev_B^{max}	Maximum leverage ratio	33.33	Based on the Basel III regulatory framework (the Basel III bank leverage can be proxied by the capital-to-assets ratio and its minimum value is 3%; since in our model the bank leverage is defined as the assets-to-capital ratio, the maximum value used is equal to 1/0.03)
lf_2	Sensitivity of the labour force-to-population ratio to hazardous waste	0.001	Selected from a reasonable range of values
lr	Rate of decline of land-use CO ₂ emissions	0.024	Taken from the DICE-2016R model (Nordhaus, 2016); has been adjusted to reflect a 1-year time step
p	Share of productivity damage in total damage caused by global warming	0.1	Selected from a reasonable range of values
\bar{p}_C	Par value of conventional corporate bonds (US\$)	100	The par value of bonds is assumed to be always equal to US\$100
\bar{p}_G	Par value of green corporate bonds (US\$)	100	The par value of bonds is assumed to be always equal to US\$100
pr	Ratio of demand-determined output to supply-determined output under the existence of supply-side constraints	0.99	Selected such that it is reasonably close to 1
r_0	Parameter of the function of credit rationing on conventional loans	1.50	Calculated from Eq. (125) using the initial values of dsr , CAR and lev_B
r_1	Parameter of the function of credit rationing on conventional loans	-0.25	Calibrated such that the model generates the baseline scenario
r_2	Parameter of the function of credit rationing on conventional loans (related to the sensitivity of credit rationing to the default rate)	2.08	Selected from a reasonable range of values
r_3	Parameter of the function of credit rationing on conventional loans (related to the sensitivity of credit rationing to the leverage ratio of banks)	0.04	Selected from a reasonable range of values
r_4	Parameter of the function of credit rationing on conventional loans (related to the sensitivity of credit rationing to the capital adequacy ratio of banks)	2.08	Selected from a reasonable range of values
rep	Loan repayment ratio	0.1	Selected from a reasonable range of values
S	Equilibrium climate sensitivity, i.e. increase in equilibrium temperature due to doubling of CO ₂ concentration from pre-industrial levels (°C)	3.1	Taken from then DICE-2016R model (Nordhaus, 2016)

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Symbol	Description	Value	Remarks/sources
s_B	Banks' retention rate	0.84	Calibrated such that the model generates the baseline scenario
s_C	Share of conventional corporate bonds held by central banks (trillion US\$)	0.01	Calculated from Eq. (138) using the initial values of B_{CCB} and B_C
s_F	Firms' retention rate	0.11	Calibrated such that the model generates the baseline scenario
s_G	Share of green corporate bonds held by central banks (trillion US\$)	0.00	Calculated from Eq. (137) using the initial values of B_{CCB} and B_C
s_W	Wage income share	0.52	Based on Penn World Table 9.0
t_1	Speed of adjustment parameter in the atmospheric temperature equation	0.020	Taken from the DICE-2016R model (Nordhaus, 2016); has been adjusted to reflect a 1-year time step
t_2	Coefficient of heat loss from the atmosphere to the lower ocean (atmospheric temperature equation)	0.018	Taken from the DICE-2016R model (Nordhaus, 2016); has been adjusted to reflect a 1-year time step
t_3	Coefficient of heat loss from the atmosphere to the lower ocean (lower ocean temperature equation)	0.005	Taken from the DICE-2016R model (Nordhaus, 2016); has been adjusted to reflect a 1-year time step
w_L	Risk weight on loans	1.0	Based on BCBS (2006)
w_S	Risk weight on government securities	0.0	Based on BCBS (2006)
x_{10}	Autonomous proportion of desired conventional investment funded via bonds	0.02	Calculated from Eq. (83) using the initial values of $yield_C$ and x_I
x_{11}	Sensitivity of the proportion of desired conventional investment funded via bonds to the conventional bond yield	0.10	Selected from a reasonable range of values
x_{21}	Sensitivity of the proportion of desired green investment funded via bonds to the green bond yield	0.10	Selected from a reasonable range of values
a_{00}	Parameter of the desired investment function	0.16	Calibrated such that the model generates the baseline scenario
a_{01}	Parameter of the desired investment function	1.18	Calibrated such that the model generates the baseline scenario
a_1	Parameter of the desired investment function (related to the sensitivity of investment to the capacity utilisation)	2.00	Based on econometric estimations for a panel of countries over the period 1950-2014 (available upon request)
a_2	Parameter of the desired investment function (related to the sensitivity of investment to the rate of profit)	1.66	Based on econometric estimations for a panel of countries over the period 1950-2014 (available upon request)
a_{31}	Parameter in the investment function (related to the sensitivity of investment to the unemployment rate)	0.02	Based on econometric estimations for a panel of countries over the period 1950-2014 (available upon request)
a_{32}	Parameter in the investment function (related to the sensitivity of investment to the unemployment rate)	0.5	Selected from a reasonable range of values
a_{41}	Parameter in the investment function (related to the sensitivity of investment to the energy utilisation rate)	0.1	Selected from a reasonable range of values
a_{42}	Parameter in the investment function (related to the sensitivity of investment to the energy utilisation rate)	0.99	Selected from a reasonable range of values
a_{51}	Parameter in the investment function (related to the sensitivity of investment to the matter utilisation rate)	0.1	Selected from a reasonable range of values
a_{52}	Parameter in the investment function (related to the sensitivity of investment to the matter utilisation rate)	0.99	Selected from a reasonable range of values
β_1	Autonomous share of desired green investment in total investment	0.02	Calibrated such that the model generates the baseline scenario
β_2	Sensitivity of the desired green investment share to the interest rate differential between green loans/bonds and conventional loans/bonds	1	Selected from a reasonable range of values
δ_0	Depreciation rate of capital stock when there are no global warming damages	0.04	Based on Penn World Table 9.0
ε^{max}	Maximum potential value of energy intensity (EJ)/trillion US\$	12	Selected such that it is reasonably higher than initial ε
ε^{min}	Minimum potential value of energy intensity (EJ)/trillion US\$	2	Selected such that it is reasonably higher than 0
ζ_1	Rate of decline of the (absolute) growth rate of CO ₂ intensity	0.0005	Calibrated such that the model generates the baseline scenario
ζ_2	Rate of decline of the growth rate of β_0	0.005	Calibrated such that the model generates the baseline scenario
ζ_3	Rate of decline of the autonomous (absolute) growth rate of labour productivity	0.02	Calibrated such that the model generates the baseline scenario
ζ_4	Rate of decline of the growth rates of x_{20} and λ_{30}	0.20	Calibrated such that the model generates the baseline scenario
ζ_5	Rate of decline of the growth rate of population	0.04	Calibrated such that the model generates the baseline scenario
ζ_6	Rate of decline of the autonomous labour force-to-population ratio	0.0006	Calibrated such that the model generates the baseline scenario
η_1	Parameter of damage function	0	Based on Weitzmann (2012); $D_T=50\%$ when $T_{AT}=6^\circ\text{C}$
η_2	Parameter of damage function	0.00284	Based on Weitzmann (2012); $D_T=50\%$ when $T_{AT}=6^\circ\text{C}$
η_3	Parameter of damage function	0.000005	Based on Weitzmann (2012); $D_T=50\%$ when $T_{AT}=6^\circ\text{C}$
λ_{10}	Parameter of households' portfolio choice	0.40	Calculated from Eq. (105) using the initial values of SEC_H , V_{HF} , D_T , $yield_C$, $yield_G$ and Y_H
λ_{10}'	Parameter of households' portfolio choice	0.10	Selected from a reasonable range of values
λ_{11}	Parameter of households' portfolio choice	0.03	Calculated from the constraint $\lambda_{11} = -\lambda_{21} - \lambda_{31} - \lambda_{41}$
λ_{12}	Parameter of households' portfolio choice	-0.01	Selected from a reasonable range of values
λ_{13}	Parameter of households' portfolio choice	-0.01	Selected from a reasonable range of values
λ_{14}	Parameter of households' portfolio choice	-0.01	Selected from a reasonable range of values
λ_{15}	Parameter of households' portfolio choice	-0.01	Selected from a reasonable range of values
λ_{20}	Parameter of households' portfolio choice	0.10	Calculated from Eq. (106) using the initial values of B_{GH} , V_{HF} , D_T , $yield_C$, $yield_G$ and Y_H
λ_{20}'	Parameter of households' portfolio choice	-0.20	Selected from a reasonable range of values
λ_{21}	Parameter of households' portfolio choice	-0.01	Calculated from the constraint $\lambda_{21} = \lambda_{12}$
λ_{22}	Parameter of households' portfolio choice	0.03	Calculated from the constraint $\lambda_{22} = -\lambda_{12} - \lambda_{32} - \lambda_{42}$
λ_{23}	Parameter of households' portfolio choice	-0.01	Selected from a reasonable range of values
λ_{24}	Parameter of households' portfolio choice	-0.01	Selected from a reasonable range of values
λ_{25}	Parameter of households' portfolio choice	-0.01	Selected from a reasonable range of values

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Symbol	Description	Value	Remarks/sources
λ_{30}	Parameter of households' portfolio choice	0.00	Global warming damages are assumed to have no impact on the holdings of green bonds
λ_{31}	Parameter of households' portfolio choice	-0.01	Calculated from the constraint $\lambda_{31} = \lambda_{13}$
λ_{32}	Parameter of households' portfolio choice	-0.01	Calculated from the constraint $\lambda_{32} = \lambda_{23}$
λ_{33}	Parameter of households' portfolio choice	0.03	Calculated from the constraint $\lambda_{33} = -\lambda_{13} - \lambda_{23} - \lambda_{43}$
λ_{34}	Parameter of households' portfolio choice	-0.01	Selected from a reasonable range of values
λ_{35}	Parameter of households' portfolio choice	-0.01	Selected from a reasonable range of values
λ_{40}	Parameter of households' portfolio choice	0.50	Calculated from the constraint $\lambda_{40} = 1 - \lambda_{10} - \lambda_{20} - \lambda_{30}$
λ_{40}'	Parameter of households' portfolio choice	0.10	Calculated from the constraint $\lambda_{40}' = -\lambda_{10}' - \lambda_{20}' - \lambda_{30}'$
λ_{41}	Parameter of households' portfolio choice	-0.01	Calculated from the constraint $\lambda_{41} = \lambda_{14}$
λ_{42}	Parameter of households' portfolio choice	-0.01	Calculated from the constraint $\lambda_{42} = \lambda_{24}$
λ_{43}	Parameter of households' portfolio choice	-0.01	Calculated from the constraint $\lambda_{43} = \lambda_{34}$
λ_{44}	Parameter of households' portfolio choice	0.03	Calculated from the constraint $\lambda_{44} = -\lambda_{14} - \lambda_{24} - \lambda_{34}$
λ_{45}	Parameter of households' portfolio choice	0.03	Calculated from the constraint $\lambda_{45} = -\lambda_{15} - \lambda_{25} - \lambda_{35}$
μ^{max}	Maximum potential value of material intensity (kg/US\$)	1.5	Selected such that it is reasonably higher than initial μ
μ^{min}	Minimum potential value of material intensity (kg/US\$)	0.3	Selected such that it is reasonably higher than 0
ζ	Proportion of durable consumption goods discarded every year	0.007	Selected such that the initial growth of DC is equal to the growth rate of output
π_1	Parameter linking the green capital-conventional capital ratio with material intensity	2.08	Calibrated such that initial μ corresponds to initial κ and $\mu(2050) = 0.9\mu(2015)$ in line with the baseline scenario
π_2	Parameter linking the green capital-conventional capital ratio with material intensity	19.98	Calibrated such that initial μ corresponds to initial κ and $\mu(2050) = 0.9\mu(2015)$ in line with the baseline scenario
π_3	Parameter linking the green capital-conventional capital ratio with recycling rate	7.61	Calibrated such that initial ρ corresponds to initial κ and $\rho(2050) = 1.4\rho(2015)$ in line with the baseline scenario
π_4	Parameter linking the green capital-conventional capital ratio with recycling rate	40.55	Calibrated such that initial ρ corresponds to initial κ and $\rho(2050) = 1.4\rho(2015)$ in line with the baseline scenario
π_5	Parameter linking the green capital-conventional capital ratio with energy intensity	13.63	Calibrated such that initial ε corresponds to initial κ and $\varepsilon(2050) = 0.7\varepsilon(2015)$ in line with the baseline scenario
π_6	Parameter linking the green capital-conventional capital ratio with energy intensity	62.74	Calibrated such that initial ε corresponds to initial κ and $\varepsilon(2050) = 0.7\varepsilon(2015)$ in line with the baseline scenario
π_7	Parameter linking the green capital-conventional capital ratio with the share of renewable energy	36.50	Calibrated such that initial θ corresponds to initial κ and $\theta(2050) = 0.25$ in line with the baseline scenario
π_8	Parameter linking the green capital-conventional capital ratio with the share of renewable energy	47.58	Calibrated such that initial θ corresponds to initial κ and $\theta(2050) = 0.25$ in line with the baseline scenario
ρ^{max}	Maximum potential value of recycling rate	0.8	Selected such that it is reasonably lower than 1
σ_1	Autonomous growth rate of labour productivity	0.0108	Calibrated such that the model generates the baseline scenario
σ_2	Sensitivity of labour productivity growth to the growth rate of output	0.92	Empirically estimated using data for a panel of countries over the period 1991-2016 (the econometric estimations are available upon request)
τ_F	Firms' tax rate	0.15	Selected from a reasonable range of values
τ_{H1}	Households' tax rate	0.14	Calibrated such that the model generates the baseline scenario
φ_{11}	Transfer coefficient for carbon from the atmosphere to the atmosphere	0.9760	Calculated from the formula $\varphi_{11} = 1 - \varphi_{12}$ (see the DICE-2016R model, Nordhaus, 2016)
φ_{12}	Transfer coefficient for carbon from the atmosphere to the upper ocean/biosphere	0.0240	Taken from the DICE-2016R model (Nordhaus, 2016); has been adjusted to reflect a 1-year time step
φ_{21}	Transfer coefficient for carbon from the upper ocean/biosphere to the atmosphere	0.0392	Calculated from the formula $\varphi_{21} = \varphi_{12}(CO2_{AT-PRE} / CO2_{UP-PRE})$ (see the DICE-2016R model, Nordhaus, 2016)
φ_{22}	Transfer coefficient for carbon from the upper ocean/biosphere to the upper ocean/biosphere	0.9595	Calculated from the formula $\varphi_{22} = 1 - \varphi_{21} - \varphi_{23}$ (see the DICE-2016R model, Nordhaus, 2016)
φ_{23}	Transfer coefficient for carbon from the upper ocean/biosphere to the lower ocean	0.0013	Taken from the DICE-2016R model (Nordhaus, 2016); has been adjusted to reflect a 1-year time step
φ_{32}	Transfer coefficient for carbon from the lower ocean to the upper ocean/biosphere	0.0003	Calculated from the formula $\varphi_{32} = \varphi_{23}(CO2_{UP-PRE} / CO2_{LO-PRE})$ (see the DICE-2016R model, Nordhaus, 2016)
φ_{33}	Transfer coefficient for carbon from the lower ocean to the lower ocean	0.9997	Calculated from the formula $\varphi_{33} = 1 - \varphi_{32}$ (see the DICE-2016R model, Nordhaus, 2016)

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