

# DEFINE-CLIMATE

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[www.define-model.org](http://www.define-model.org)

## 1. Brief description

DEFINE-CLIMATE is a simplified module of DEFINE, which shows how climate change is affected by economic activity. Higher economic growth leads to a generation of higher carbon emissions (for a given level of energy intensity, carbon intensity, sequestration rate and share of renewables). These carbon emissions cumulative carbon emissions which in turn increase atmospheric temperature.

## 2. Module equations

$$\text{Output: } Y_t = Y_{t-1}(1 + g_Y) \quad (1)$$

$$\text{Total energy: } E_t = \varepsilon Y_t \quad (2)$$

$$\text{Fossil energy: } E_{Ft} = (1 - \theta) E_t \quad (3)$$

$$\text{Industrial CO}_2 \text{ emissions: } EMIS_{INt} = \omega(1 - seq) E_{Ft} \quad (4)$$

$$\text{Land-use CO}_2 \text{ emissions: } EMIS_{Lt} = EMIS_{Lt-1}(1 - g_{EMISL}) \quad (5)$$

$$\text{Growth rate of land-use CO}_2 \text{ emissions: } g_{EMISL} = g_{EMISL-1}(1 - \zeta_9) \quad (6)$$

$$\text{Total emissions: } EMIS_t = EMIS_{INt} + EMIS_{Lt} \quad (7)$$

$$\text{Cumulative CO}_2 \text{ emissions: } CO2_{CUMt} = CO2_{CUMt-1} + EMIS_t \quad (8)$$

$$\text{Atmospheric temperature: } T_{ATt} = T_{ATt-1} + t_1(t_2 \phi CO2_{CUM-1} - T_{ATt-1}) \quad (9)$$

### 3. Symbols and values

Symbol	Description	Value/calculation
<b>Parameters</b>		
$g_Y$	Growth rate of GDP	0.029
$\epsilon$	Energy intensity, i.e. energy use per unit of GDP (EJ/trillion US\$)	Calculated from equation (2)
$\theta$	Share of non-fossil energy in total energy	0.15
$\omega$	CO <sub>2</sub> intensity, i.e. CO <sub>2</sub> emissions per unit of non-renewable energy use (Gt/EJ)	Calculated from equation (4)
$seq$	Proportion of carbon that is sequestered	0.002186
$\zeta_g$	Rate of decline of the growth rate of $EMIS_L$	0.0140
$t_1$	Coefficient capturing the timescale of the initial adjustment of the climate system to an increase in cumulative emissions	0.5
$t_2$	Coefficient that captures the global warming that stems from non-CO <sub>2</sub> greenhouse gas	1.1
$\varphi$	Transient Climate Response to cumulative carbon Emissions (TCRE) (°C/GtCO <sub>2</sub> )	0.0005
<b>Endogenous variables</b>		
$Y$	Output (trillion US\$)	85.9
$E$	Energy used for the production of output (EJ)	590.0
$E_F$	Energy produced from fossil sources (EJ)	Calculated from equation (3)
$EMIS_{IN}$	Industrial CO <sub>2</sub> emissions (GtCO <sub>2</sub> )	36.6
$EMIS_L$	Land-use CO <sub>2</sub> emissions (GtCO <sub>2</sub> )	5.5
$g_{EMISL}$	Growth rate of land emissions	0.016
$EMIS$	Total CO <sub>2</sub> emissions (GtCO <sub>2</sub> )	Calculated from equation (7)
$CO2_{CUM}$	Cumulative CO <sub>2</sub> emissions (GtCO <sub>2</sub> )	2210
$T_{AT}$	Atmospheric temperature over pre-industrial levels (°C)	1.14

### 4. Steps for simulating the model in R

#Open R and create a new R script (File->New file->R script). Save this file as 'Climate' (File->Save as).

#Clear the workspace and identify how many time periods (T) you wish your model to run (once you write the commands, press 'Source')

```
rm(list=ls(all=TRUE))
T<-83
```

#STEP 1: For each endogenous variable, create a vector that has a length equal to the time periods. (Once you have written the commands, press 'Source'.)

#### #Endogenous variables

```
Y<- vector(length=T)
E<- vector(length=T)
E_F<- vector(length=T)
EMIS_IN<- vector(length=T)
EMIS_L<- vector(length=T)
EMIS<- vector(length=T)
g_EMIS_L<- vector(length=T)
CO2_CUM<- vector(length=T)
T_AT<- vector(length=T)
```

**#STEP 2: Give values to the parameters (use the values reported in the table in Section 3).**

#### #Parameters

```
for (i in 1:T) {  
  if (i == 1) {  
    for (iterations in 1:10){  
      g_Y<-0.029  
      epsilon <- E[i]/Y[i] #EJ/trillion US$  
      theta<-0.15  
      omega<-EMIS_IN[i]/E_F[i] #Gt/EJ  
      seq<- 0.002186  
      zeta_9<-0.014  
      t_1<- 0.5  
      t_2<- 1.1  
      phi<-1.72/(3.667*1000)
```

**#STEP 3: Give values to your initial variables (use the values reported in the table in Section 3).**

#### #Initial values

```
Y[i] <- 85.9 #trillion US$  
E[i]<-590 #EJ  
E_F[i]<-(1-theta)*E[i] #EJ  
EMIS_IN[i]<-36.6 #Gt  
EMIS_L[i] <-5.5 #Gt  
g_EMIS_L[i]<-0.016  
EMIS[i]<- EMIS_IN[i]+EMIS_L[i] #Gt  
CO2_CUM[i]<-2210 # GtCO2  
T_AT[i] <-1.14 #°C  
}  
}
```

**#STEP 4: Write down the equations and run the model. (Once you have written the commands, press 'Source'.)**

#### #Equations

```
else {
```

```
for (iterations in 1:10){
```

```
Y[i] <- Y[i-1]*(1+g_Y) #Eq. (1)  
E[i] <- epsilon*Y[i] #Eq. (2)  
E_F[i] <- (1-theta)*E[i] #Eq. (3)  
EMIS_IN[i] <- omega*(1-seq)*E_F[i] #Eq. (4)  
EMIS_L[i]<- EMIS_L[i-1]*(1-g_EMIS_L[i]) #Eq. (5)  
g_EMIS_L[i]<-g_EMIS_L[i-1]*(1-zeta_9) #Eq. (6)  
EMIS[i] <- EMIS_IN[i]+EMIS_L[i] #Eq. (7)  
CO2_CUM[i]<-CO2_CUM[i-1]+EMIS[i] #Eq. (8)  
T_AT[i]<-T_AT[i-1]+t_1*(t_2*phi*CO2_CUM[i-1]-T_AT[i-1]) #Eq. (9)
```

```
}  
}  
}
```

**#STEP 5: Create a table to report the following variables: Y, E\_F, EMIS\_IN, EMIS, CO2\_CUM, T\_AT. Create also 3 graphs for the variables Y, EMIS and T\_AT. (Once you have written the commands, press 'Source'.)**

### #Table

```
matrixname<-paste("Table")  
assign (matrixname, (round(cbind(Y, E_F, EMIS_IN, EMIS, CO2_CUM, T_AT), digits=4)))  
  
plot(Table[1:83,c("Y")], type="l", xlab= "Year", ylab="Output (trillion US$)", xaxt="n")  
axis(side=1, at=c(1, 13, 23, 33, 43, 53, 63, 73, 83), labels=c("2018", "2030", "2040", "2050", "2060",  
"2070", "2080", "2090", "2100"))  
  
plot(Table[1:83,c("EMIS")], type="l", xlab= "Year", ylab=expression("CO" [2]*" emissions  
(Gt)"),xaxt="n")  
axis(side=1, at=c(1, 13, 23, 33, 43, 53, 63, 73, 83), labels=c("2018", "2030", "2040", "2050", "2060",  
"2070", "2080", "2090", "2100"))  
  
plot(Table[1:83,c("T_AT")], type="l", xlab= "Year", ylab=expression("Temperature ("^{0}*"C above  
pre-industrial)"), xaxt="n")  
axis(side=1, at=c(1, 13, 23, 33, 43, 53, 63, 73, 83), labels=c("2018", "2030", "2040", "2050", "2060",  
"2070", "2080", "2090", "2100"))
```